Regional Cooperation for Limited Area Modeling in Central Europe



ACC 🚋 RD

A Consortium for COnvection-scale modelling Research and Development

# Dynamics for ACCORD model higher numerical stability

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Czech Hydrometeorological Institute











Dynamical core in ACCORD

**SI** time scheme

• Orographic terms in linear model (based on ideas of Fabrice Voitus and Jozef Vivoda)

□ Idealised test cases

Real simulations @200m





**Basic equations** 

□ hydrostatic primitive equation system (HPE) or Euler equations (EE); recently implemented quasi elastic equation system (QE)

**D** prognostic variables  $\vec{v}, T, q_s = \ln(\pi_s)$ , in EE with  $w, \hat{q} = \ln(\frac{p}{\pi})$ 

Discretization

- **u** spectral method for horizontal direction
- □ hybrid vertical coordinate  $\eta$  based on hydrostatic pressure  $\pi(\eta) = A(\eta) + B(\eta)\pi_s$ ; A(top) = B(top) = 0, A(bottom) = 0, B(bottom) = 1
- □ finite differences or finite elements for vertical direction discretization
- □ semi-implicit or iterative centred implicit scheme for time discretization
- semi-Lagrangian advection



## Semi-Implicit time scheme



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Using linear model  $\mathcal{L}^*$  we divide

$$\frac{dX}{dt} = \mathcal{L}^* \overline{[X]}^t + (\mathcal{M} - \mathcal{L}^*) X$$

and discretize in time to obtain

$$\frac{\mathbf{X}^{+} - \mathbf{X}^{0}}{\Delta t} = \mathcal{L}^{*}\left(\frac{\mathbf{X}^{+} + \mathbf{X}^{0}}{2}\right) + (\mathcal{M} - \mathcal{L}^{*})\mathbf{X}^{+\frac{1}{2}}$$

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 $X = \mathbf{X}^* + \mathbf{X}', \quad \mathcal{M} \longrightarrow \mathcal{L}^*$ 

or

$$\frac{\mathbf{X}^{+(n)} - \mathbf{X}^{0}}{\Delta t} = \frac{\mathcal{L}^{*} \mathbf{X}^{+(n)} + \mathcal{L}^{*} \mathbf{X}^{0}}{2} + \frac{(\mathcal{M} - \mathcal{L}^{*}) \mathbf{X}^{+(n-1)} + (\mathcal{M} - \mathcal{L}^{*}) \mathbf{X}^{0}}{2}$$

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Semi-implicit scheme

Linearization

We know that both can be second order accurate in time when some care is taken (averaging along semi-Lagrangian trajectory).

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Iterative centered implicit scheme

# **Full model**



#### Temperature

$$\frac{dT}{dt} = \frac{\kappa T}{\kappa - 1} \left( D + d \right)$$

#### Horizontal momentum

$$\frac{d\vec{v}}{dt} = -RT\frac{\nabla\pi}{\pi} - \nabla\phi - RT\nabla\hat{q} - \frac{1}{m}\frac{\partial(p-\pi)}{\partial\eta}\nabla\phi$$

Vertical	momen	tum	
	$\frac{dw}{dt} =$	$\frac{g}{m}\frac{\partial(p-\tau)}{\partial\eta}$	r)

#### Pressure departure

$$\frac{d\hat{q}}{dt} = \frac{1}{\kappa - 1} \left( D + d \right) - \frac{1}{\pi} \frac{d\pi}{dt}$$

#### Surface pressure

$$rac{dq_s}{dt} = -rac{1}{\pi_s} \int_0^1 
abla \cdot (m ec v) d\eta$$

#### Diagnostic relations

$$\frac{d\pi}{dt} = \vec{v} \cdot \nabla \pi - \int_0^{\eta} \nabla \cdot (m\vec{v}) d\eta'$$
$$\phi = \phi_s - \int_{\eta}^1 \frac{mRT}{p} d\eta'$$
$$d = \frac{p}{mRT} \left( \nabla \phi \frac{\partial \vec{v}}{\partial \eta} - g \frac{\partial w}{\partial \eta} \right)$$

D	=	$ abla \cdot ec v$
$\kappa$	=	$rac{c_p}{R}$
m	=	$rac{\partial \pi}{\partial \eta}$
	D $\kappa$ m	D = $\kappa =$ m =

# **Full model**



#### Temperature

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#### Horizontal momentum

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Definitions			
	D	=	$ abla \cdot ec v$
	$\kappa$	=	$rac{c_p}{R}$
	m	=	$rac{\partial\pi}{\partial\eta}$



Current:

stationary

resting

 $\Box$  hydrostatically balanced ( $\pi_s^*$ )

🖵 dry

 $\Box$  isothermal ( $T^*$ )

 $\Box$  with constant orography ( $\nabla \phi^* = 0$ )







New:

stationary

resting

 $\Box$  hydrostatically balanced ( $\pi_s^*$ )

🖵 dry

□ isothermal (*T*<sup>\*</sup>)

 $\Box$  with constant orographic slope (in absolute value,  $|\nabla \phi^*| \neq 0$ )



### Linear model



#### Temperature

$$\frac{\partial T}{\partial t} = \frac{\kappa T^*}{\kappa - 1} \left( D + d \right)$$

#### Horizontal momentum

$$\frac{\partial \vec{v}}{\partial t} = -RT^* \frac{\nabla \pi}{\pi^*} - \nabla \phi - RT^* \nabla \hat{q} - \frac{1}{m^*} \frac{\partial \pi^* \hat{q}}{\partial \eta} \nabla \phi^*$$

/ertical	mom	entum		
	$\frac{\partial w}{\partial t}$	$= \frac{g}{m^*}$	$rac{\partial \pi^* \widehat{q}}{\partial \eta}$	

#### Pressure departure

$$\frac{\partial \hat{q}}{\partial t} = \frac{1}{\kappa - 1} \left( D + d \right) + \frac{1}{\pi^*} \int_0^{\eta} m^* D d\eta'$$

# Surface pressure $\frac{\partial q_s}{\partial t} = -\frac{1}{\pi_s^*} \int_0^1 m^* D d\eta$

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Definitions

#### Diagnostic relations

$$\nabla \phi^* = \nabla \phi^*_s - \int_{\eta}^{1} \nabla \left(\frac{m^* R T^*}{\pi^*}\right) d\eta'$$
  
$$\nabla \phi^*_s = g \wedge^*$$
  
$$d = \frac{\pi^*}{m^* R T^*} \left(\nabla \phi^* \frac{\partial \vec{v}}{\partial \eta} - g \frac{\partial w}{\partial \eta}\right)$$

# New SI parameter $\Lambda^* = \frac{1}{g} \max (||\nabla \phi_s||, \text{over domain})$ $m^* = \frac{\partial \pi^*}{\partial \eta}$



□ formulate time evolution for the modified vertical divergence

- $\Box$  omit the first order terms in  $\nabla \phi^*$ , then  $\frac{\partial \vec{v}}{\partial t}$  is unchanged and all operators of the RHS of  $\frac{\partial d}{\partial t}$  apply on  $\hat{q}$
- $\Box$  formulate RHS of  $\frac{\partial d}{\partial t}$  as new vertical Laplacian operator applied on  $\hat{q}$
- with no slopes present the new vertical Laplacian collapses to the old one
- □ new vertical Laplacian has only real and negative eigenvalues in "reasonable cases"
- □ discretize (we omit the details here)
- eliminate all variables up to horizontal divergence D
- $\Box$  solve the Helmholtz equation for D as usually





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Vertical velocity for the uniform wind over an Agnesi shaped mountain with increasing slope,  $max(||\nabla \phi_s||) = 0.6$ 



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GW

SHM



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SHMU

Vertical velocity for the uniform wind over an Agnesi shaped mountain with increasing slope,  $max(||\nabla \phi_s||) = 0.9$ 



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Vertical velocity for the uniform wind over an Agnesi shaped mountain with increasing slope,  $max(||\nabla \phi_s||) = 1.2$ 



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Vertical velocity for the uniform wind over an Agnesi shaped mountain with increasing slope,  $max(||\nabla \phi_s||) = 1.5$ 



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Vertical velocity for the uniform wind over an Agnesi shaped mountain with increasing slope,  $max(||\nabla \phi_s||) = 1.8$ 



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Vertical velocity for the uniform wind over an Agnesi shaped mountain with increasing slope,  $max(||\nabla \phi_s||) = 2$ 

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Vertical velocity for the uniform wind over an Agnesi shaped mountain with increasing slope,  $max(||\nabla \phi_s||) = 2.4$ 

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Vertical velocity for the uniform wind over an Agnesi shaped mountain with increasing slope,  $max(||\nabla \phi_s||) = 3$ 





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**72**°



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Vertical velocity for the uniform wind over an Agnesi shaped mountain with increasing slope,  $max(||\nabla \phi_s||) = 3.5$ 

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$$\Lambda^* = 0.$$



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Vertical velocity for the uniform wind over an Agnesi shaped mountain with increasing slope,  $max(||\nabla \phi_s||) = 4$ 

$$\Lambda^* = 0.$$





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□ The ICI scheme in ACCORD uses horizontally constant coefficients.

In 
$$\frac{dX}{dt} = \mathcal{L}^* \overline{[X]}^t + (\mathcal{M} - \mathcal{L}^*)X$$

the linear model  $\mathcal{L}^*$  is just a matrix with numbers, constant during the whole integration.

- □ The Helmholtz matrix calculated from it is constant in time and applied in spectral space on spectral coefficients.
- □ It means that we chose just one value for each of the reference parameters in the linear model, being the same in the whole domain.
- □ With the added reference slope it is the same one value is chosen for the whole domain.
- □ It follows that we must chose a value which will work well in flat terain too.





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Vertical velocity for the uniform wind over an Agnesi shaped mountain with very small height,  $max(||\nabla \phi_s||) = 0.1$ 



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Vertical velocity for the uniform wind over an Agnesi shaped mountain with very small height,  $max(||\nabla \phi_s||) = 0.1$ 



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Vertical velocity for the uniform wind over an Agnesi shaped mountain with very small height,  $max(||\nabla \phi_s||) = 0.1$ 



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 $\Lambda^* = 0.$ 

 $\Lambda^* = 3.$ 



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Vertical velocity for the uniform wind over an Agnesi shaped mountain with very small height,  $max(||\nabla \phi_s||) = 0.1$ 



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 $\Lambda^* = 0.$ 

 $\Lambda^* = 4.$ 



The basic algorithmic choices for ALARO configurations are:

- semi-Lagrangian advection with 4 iterations for trajectory calculation
- PC time scheme with one iteration, cheap variant (SL trajectories are not recalculated in corrector)
- modified vertical divergence d4 for vertical motion, transformation to vertical velocity w in the non-linear model
- reference values of the linear model: SITR=300K, SITRA=100K, SIPR=900hPa
- no decentering
- semi-Lagrangian horizontal diffusion applied on all model variables + TKE,TTE, hydrometeors
- linear truncation for all spectral fields except orography; quadratic truncation of orography

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#### **ALARO** physics

- □ radiation scheme ACRANEB2
- □ turbulence and shalow convection scheme TOUCANS, model 2
- □ scale aware deep convection and microphysics scheme 3MT

#### Initialization

□ initialization with 3DVAR + surface DA (CANARI) for 2.325km run; dynamical adaptation + DFI for 500m and 200m runs

Particular choices for ALARO@200m:

- **u** cubic truncation of orography
- SITRA=50K
- □ no 3MT (deep convection), only STRAPRO (stratiform precipitation)





#### Vertical velocity for the alpine case 19 August 2022 OUTC + 24hours.







Vertical velocity for the alpine case 19 August 2022 OUTC + 24hours.

 $\Lambda^* = 0$ 

 $\Lambda^* = 1$ 

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#### Conclusions

- □ Including constant reference slope in the linear model of the ICI time scheme helps to improve stability.
- □ With moderate values of the reference slope the accuracy of results is not endangered.
- □ With very high values of the reference slope the results may be spoiled with noise.



Děkuji Vám za pozornost!

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