

## **First attempts to implement horizontal features to the turbulence scheme TOUCANS of ACCORD/ALARO**

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- ▶ The turbulence scheme TOUCANS in ACCORD/ALARO
- ▶ Towards the 3D turbulence and the grey zone
- ▶ Prognostic equations in TOUCANS
- ▶ Horizontal features in TOUCANS
  - ▶ Horizontal turbulent length scale  $L_H$
  - ▶ Computation of the PBL height
  - ▶ Current status of the implementation
- ▶ Real case study
  - ▶ Vertical shear production and  $L_H$
  - ▶ Horizontal shear production and TKE
  - ▶ Vertical profiles
- ▶ Conclusions

(J.F.Geleyn, I.Bašták Ďurán et al.)

T - **T**hird

O - **O**rder moments

U - **U**nified

C - **C**ondensation

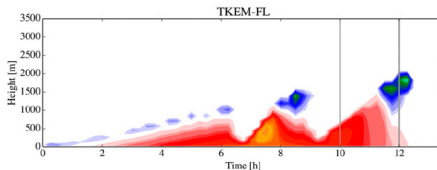
A - **A**ccounting and

N - **N**-dependent

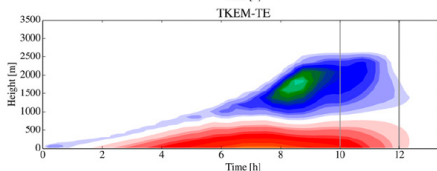
S - **S**olver for turbulence and diffusion

- ▶ uses two prognostic energies - TKE and  $TTE=TKE+TPE$
- ▶ TPE is used only for a modification of the stability parameters
- ▶ the vertical turbulent fluxes are proportional to the local gradients of the diffused variables, but the stability parameters and the turbulent exchange coefficients are not strictly local anymore and have a prognostic character
- ▶ these characteristics enable the scheme to model both turbulence and clouds in the planetary boundary layer

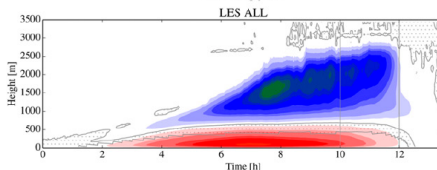
TKE



TKE  
+TTE



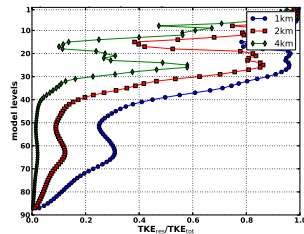
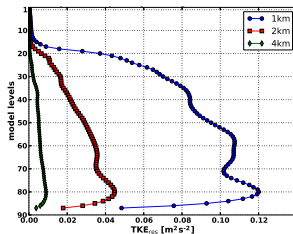
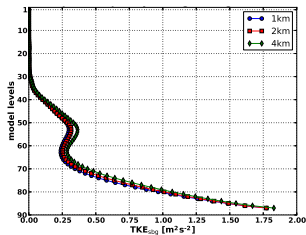
LES



The two-energy scheme shows a more continuous behavior in time and space and mixes deeper in accordance with the LES results.

(courtesy of I.Bašták)

- ▶ The existing turbulence schemes in NWP models are intended for use in horizontally homogeneous and flat terrain (1D)
- ▶ At  $\Delta x \approx 1$  km and in complex (mountainous) terrain the turbulence intensity is typically underestimated - need for 3D effects
- ▶ Furthermore, at  $\Delta x \approx 1$  km we are within the gray zone (turb. is partly resolved) - need to take care of partitioning between  $TKE_{res}$  and  $TKE_{sbg}$



for the turbulent kinetic and the turbulent total energy [Ďurán et al. (2018)]

$$\frac{de_k}{dt} = -g \frac{\partial}{\partial p} \left( \rho K_{e_k} \frac{\partial e_k}{\partial z} \right) + I + II - \frac{e_k^{\frac{3}{2}}}{\tau_k}$$
$$\frac{de_t}{dt} = -g \frac{\partial}{\partial p} \left( \rho K_{e_t} \frac{\partial e_t}{\partial z} \right) + I - \frac{e_t^{\frac{3}{2}}}{\tau_t}$$

The shear production term

$$I = -\overline{u'w'} \frac{\partial \bar{u}}{\partial z} - \overline{v'w'} \frac{\partial \bar{v}}{\partial z}$$

The buoyancy production/destruction term

$$II = E_{s_L} \overline{s_{sL}' w'} + E_{q_t} \overline{q_t' w'}$$

in the turbulent kinetic and the turbulent total energy prognostic equations  
[Goger et al. (2018, 2019)]

$$\frac{de_k}{dt} = -g \frac{\partial}{\partial p} \left( \rho K_{e_k} \frac{\partial e_k}{\partial z} \right) + I + II - \frac{e_k^{\frac{3}{2}}}{\tau_k}$$
$$\frac{de_t}{dt} = -g \frac{\partial}{\partial p} \left( \rho K_{e_t} \frac{\partial e_t}{\partial z} \right) + I - \frac{e_t^{\frac{3}{2}}}{\tau_t}$$

The shear production term

$$I = -\overline{u'w'} \frac{\partial \bar{u}}{\partial z} - \overline{v'w'} \frac{\partial \bar{v}}{\partial z} - \overline{u'u'} \frac{\partial \bar{u}}{\partial x} - \overline{u'v'} \frac{\partial \bar{u}}{\partial y} - \overline{u'v'} \frac{\partial \bar{v}}{\partial x} - \overline{v'v'} \frac{\partial \bar{v}}{\partial y}$$

The buoyancy production/destruction term

$$II = E_{s_L} \overline{s_{sL}' w'} + E_{q_t} \overline{q_t' w'}$$



The horizontal shear production term

$$HSP = L_H^2 \cdot \left[ \left( \frac{\partial u}{\partial x} \right)^2 + \left( \frac{\partial v}{\partial y} \right)^2 + \frac{1}{2} \left( \frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right)^2 \right]^{\frac{3}{2}}$$

APPROACH 1: Constant horizontal length scale

[Smagorinski (1963), Goger (2018)]

$$L_H = c_s \Delta x, \quad c_s = 0.2.$$

It is too simple and appropriate only for small scale processes which are isotropic.

## APPROACH 2: Variable horizontal length scale [Goger et al. (2019)]

$$L_H = W \cdot T_{L,u,v}, \quad T_{L,u,v} = 0.15 \frac{H_{PBL}}{\sigma_{u,v}}$$

$W$  - mean horizontal wind speed,  $T_{L,u,v}$  - Lagrangian integral time scale  
 $H_{PBL}$  - the height of PBL,  $\sigma_{u,v}$  - the zonal and meridional wind variances

$$\sigma_u^2 = u_*^2 \left( 5 - 4 \frac{z}{H_{PBL}} \right) + 0.35 u_*^2 \left( \frac{H_{PBL}}{\kappa L} \right)^{\frac{2}{3}}$$
$$\sigma_v^2 = u_*^2 \left( 2 - 2 \frac{z}{H_{PBL}} \right)$$

inapplicable above the PBL + based on a specific dataset

\* additional term in statically unstable conditions

None of the existing methods estimates the  $H_{PBL}$  accurately enough for different stability conditions

Weak-capping-inversion (WCI)  
[Ayotte et al. (1996)]

TKE-based method  
[Kosović and Curry (2000)]

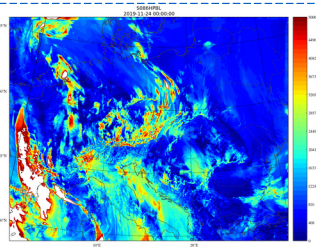
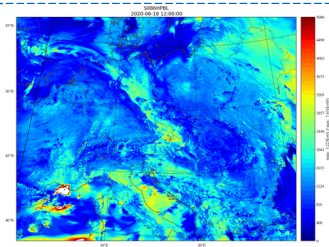
$$\langle \theta(z) \rangle_L \geq \frac{1}{z} \int_0^{z_i} \langle \theta(z) \rangle dz + 0.25$$

$$H_{PBL} = \frac{z_{05}}{0.95}$$

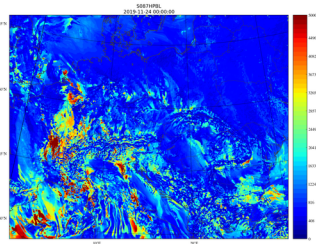
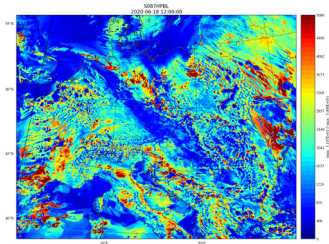
is appropriate for convective  
and near-neutral PBL

is more general (suitable for  
statically stable conditions)

# Computation of the PBL height



WCIM method



TKE-based method

(courtesy of  
M.Hrastinski)

- ▶ WCIM provides unrealistic values in statically stable conditions, while TKE-based method is characterized by grainy patterns
- ▶ Can a combination of two methods work?
- ▶ We need a more robust method, e.g. [Bašták et al. (2022)]

$$H_{PBL} = c_{pblh} \cdot \sqrt{\int_{z=0}^{z_{top}} L_{up} \cdot dz}, \quad c_{pblh} = 1.75$$

$L_{up}$  depends on stratification and turbulence within the entire model column

APPROACH 3: Horizontal length scale depending on properties of the local flow [Wang et al. (2021)] based on the length scales for shear and stretching

$$L_{Hshr} = sW \left[ \left( \frac{\partial v}{\partial x} \right)^2 + \left( \frac{\partial u}{\partial y} \right)^2 \right]^{-\frac{1}{2}}, \quad L_{Hstr} = sW \left[ \left( \frac{\partial u}{\partial x} \right)^2 + \left( \frac{\partial v}{\partial y} \right)^2 \right]^{-\frac{1}{2}}$$
$$s = \left( \frac{\Delta_0}{\Delta x} \right)^\alpha, \quad L_H = \sqrt{L_{Hshr} L_{Hstr}}$$

where  $\Delta_0$  is the grid spacing at which the model can resolve the most energetic turbulent eddies and  $\alpha = 1.45$  is an empirical constant based on the fit with observations.

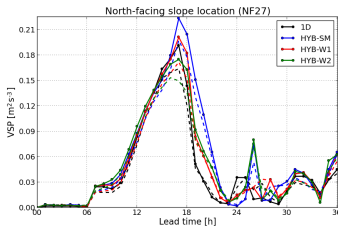
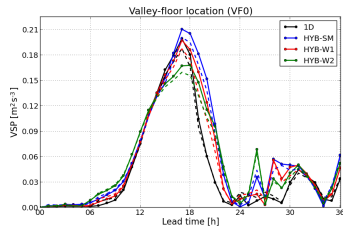
## in ACCORD/ALARO and future plans

- ▶ APPROACH 1 [Goger (2018)] and APPROACH 3 [Wang (2021)] are coded and validation is ongoing
- ▶ we do not have satisfactory results with the APPROACH 2 so far; we plan to implement APPROACH 2 [Goger (2019)] with  $\sigma_{u,v}$  computed from TOUCANS
- ▶ we plan to implement the optimal  $L_H$  option into 1D+2D turbulence scheme based on SLHD
- ▶ we plan the adaptation of TOUCANS for the grey zone (scale-aware scheme) following [Boutle et al. (2014), Honnert (2011, 2019, 2020)]

A case of 1 July 2015, 00 UTC

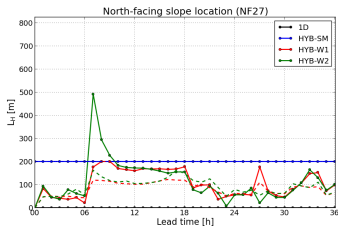
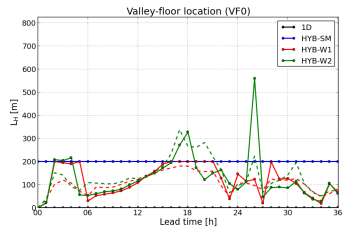
- ▶ forecast for 72 hours in the cascade of resolutions 4km, 2km, 1km approximately over the same domain covering Central Europe
- ▶ 87 vertical levels
- ▶ ALARO configuration
- ▶ coupling to ARPEGE in 3h coupling frequency





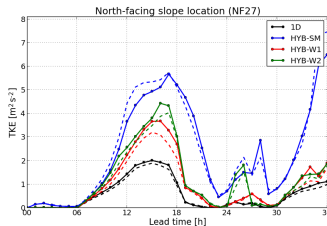
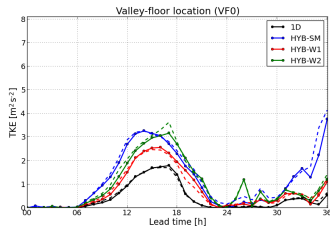
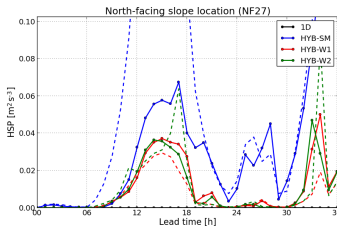
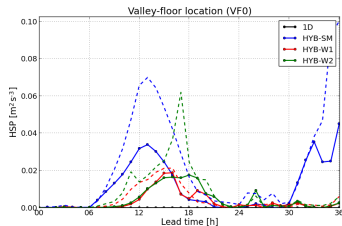
Vertical shear production

1D  
 APPROACH 1  
 APPROACH 3  
 APPROACH 3  
 bounded



Turbulent horizontal length  
 scale  $L_H$  @1km

(courtesy of M.Hrastinski)

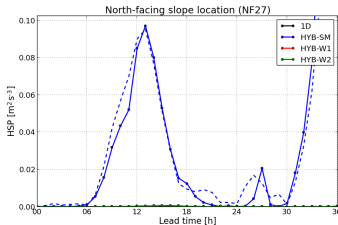
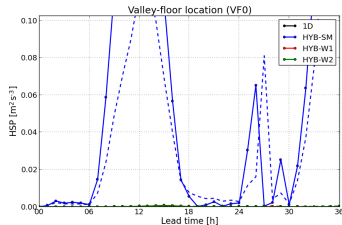


Horizontal shear production

1D  
**APPROACH 1**  
**APPROACH 3**  
**APPROACH 3**  
 bounded

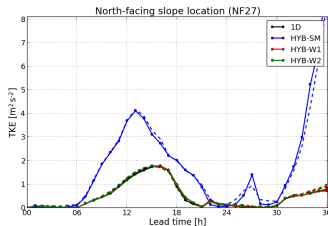
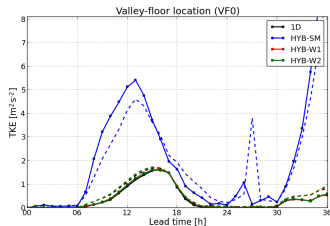
Turbulent kinetic energy  
 @1km

(courtesy of M.Hrastinski)



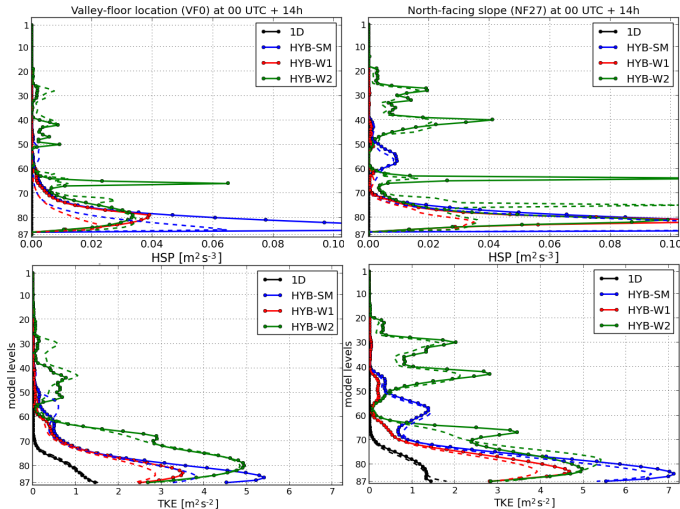
Horizontal shear production

1D  
APPROACH 1  
APPROACH 3  
APPROACH 3  
bounded



Turbulent kinetic energy  
@2km

(courtesy of M.Hrastinski)



Horizontal shear production

1D  
APPROACH 1  
APPROACH 3  
APPROACH 3  
bounded

Turbulent kinetic energy  
@1km

(courtesy of M.Hrastinski)

- ▶ There were no problems with numerical instability with any of the three tested  $L_H$  options. Spectral norms gradually develop within the first few hours of the forecast with no significant differences between 1D and quasi-3D until the intensity of turbulence reaches its maximum (early afternoon).
- ▶ The impact of the quasi-3D turbulence scheme at coarser horizontal resolution ( $\Delta x = 2\text{ km}$  and  $\Delta x = 4\text{ km}$ ) is almost negligible.
- ▶ The performance of constant  $L_H$  worsens as  $\Delta x$  increases. The Horizontal Shear Production (HSP) values are too high for the north-facing slope location and even comparable with the Vertical Shear Production (VSP).

- ▶ When variable  $L_H$  is employed, the values become comparable, pronounced daily variability is shown, with maxima near the sunrise and noon. The TKE values are slightly higher with the variable  $L_H$  formulations than for 1D. Strong HSP appears near the surface and the turbulence intensity is higher throughout the whole model column for both the valley-floor and the north-facing slope locations than for the 1D scheme.
- ▶ The third approach to  $L_H$ , which allows stronger horizontal mixing, is also able to produce a secondary and a tertiary maxima in the middle and the upper troposphere. Further research will aim on the potential benefit for the simulation of the jet stream related turbulence, as well as for lateral mixing at the edges of atmospheric fronts.

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