# Dynamics & Coupling 2007-2008 progress report

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**CHMI** 





### Work of: J. Mašek (Sk) and F. Váňa (Cz)

The Lagrangian cubic interpolation is replaced by a general two-parametric interpolator:

$$F(x, \mathbf{y}) = w_0(x)y_0 + w_1(x)y_1 + w_1(1-x)y_2 + w_0(1-x)y_3$$
 where  $\mathbf{y} = (y_0, y_1, y_2, y_3)$  
$$w_0(x) = a_1x + a_2x^2 - (a_1 + a_2)x^3$$
 
$$w_1(x) = 1 + (a_2 - 1)x - (3a_1 + 4a_2)x^2 + 3(a_1 + a_2)x^3$$



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• Any interpolator F in  $(a_1,a_2)$  plane can be composed as a linear combination of (three) other interpolators:

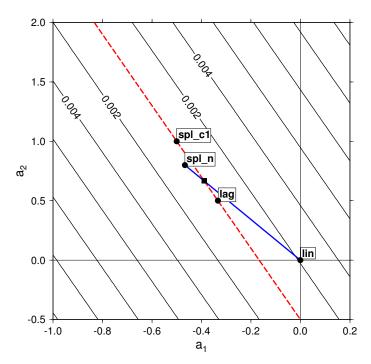
$$F = \kappa_1 F_1 + \kappa_2 F_2 + (1 - \kappa_1 - \kappa_2) F_3$$

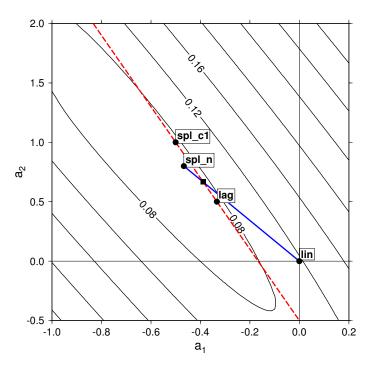


## Mean absolute error of interpolation

Mean absolute error of interpolators,  $w = \exp(-25.m/M)$ 

Mean absolute error of interpolators,  $w = \exp(-m/M)$ 





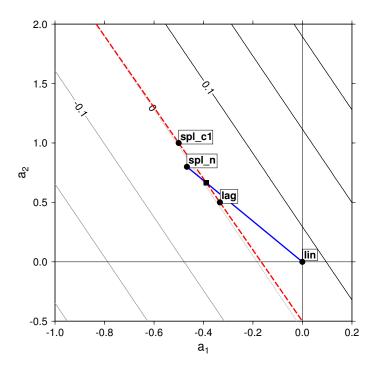


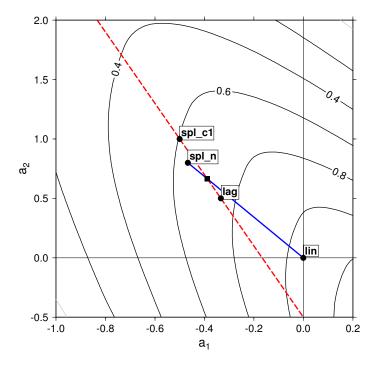


### Dimensionless damping rate

Damping factor for N = 100, m = 10

Damping factor for N = 100, m = 40







GMT 2007 Apr 20 08:43:48

#### Implementation guidelines

• The implemented scheme allows at least  $2^{nd}$  order accuracy (given by  $6a_1 + 2a_2 = -1$ ), leaving just one tunable parameter to control the interpolation property.



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$$F = F_{lag} + \kappa (F_{quad} - F_{lag})$$



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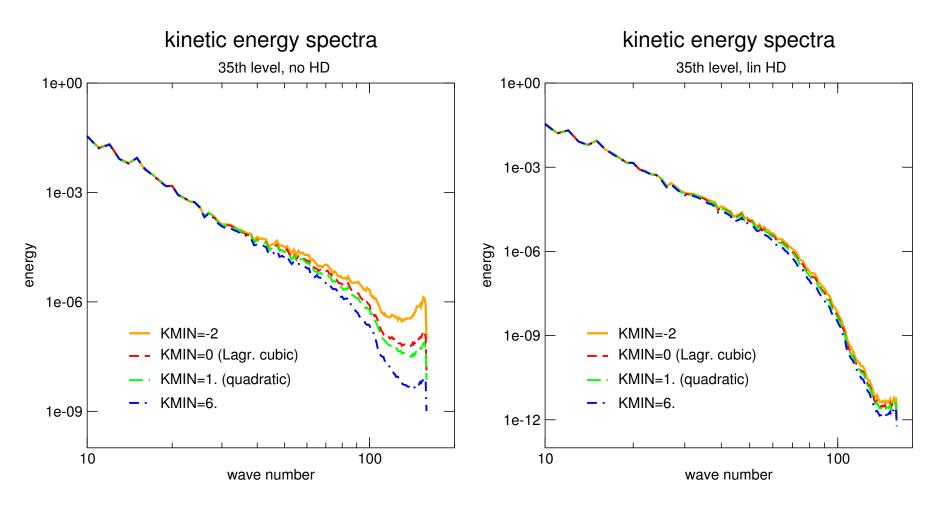
$$F = F_{lag} + \kappa (F_{quad} - F_{lag})$$

- Two sets of interpolators can be asked for simultaneously.
- The new data-flow (including the TL/AD code) is available from CY35T1.





#### 3h adiabatic forecast







Work of: J. Mašek (Sk), F. Váňa (Cz) and P. Bénard (Fr)

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 with  $\kappa = \kappa(d, ...)$ .





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- The triggering function  $\kappa$  can be optionally computed along true p-surfaces (using chain rule to evaluate horizontal derivatives) in order to prevent spurious circulation above sloped terrain.





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- Optionally the 3D grid-point laplacian is available as the damping operator.

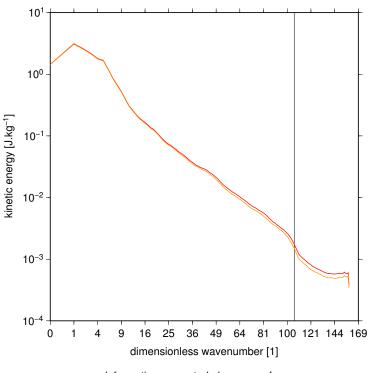




#### Impact of horizontal triggering, Alps $\Delta x$ =2.5 km

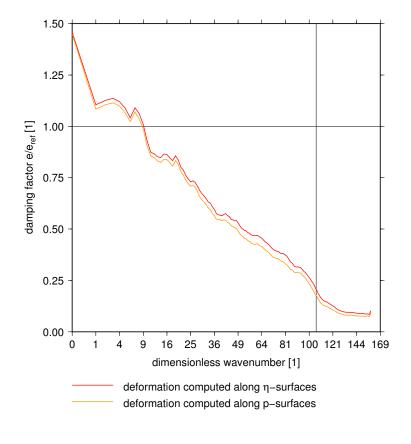
Kinetic energy spectrum (+0006 hour forecast, model level 041)

Spectral damping by SLHD scheme (+0006 hour forecast, model level 041)



deformation computed along η-surfaces deformation computed along p-surfaces

NO33,10045 LACE





#### Laplacian transformed to weights

Applying  $2^{nd}$  order diffusion to interpolated quantity y:

$$\tilde{y} = (1 + \varepsilon \Delta x^2 \partial_x^2) y$$
  
=  $(1 + \varepsilon \Delta x^2 \partial_x^2) w_1 (y_1 - y_0) + w_2 (y_2 - y_0) + w_3 (y_3 - y_0)$ 



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The diffusion operator can be transformed into weights:

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with 
$$\begin{pmatrix} \tilde{w_1} \\ \tilde{w_2} \\ \tilde{w_3} \end{pmatrix} = \begin{pmatrix} 1 - 2\varepsilon & \varepsilon & 0 \\ \varepsilon & 1 - 2\varepsilon & 0 \\ 0 & \varepsilon & 1 \end{pmatrix} \cdot \begin{pmatrix} w_1 \\ w_2 \\ w_3 \end{pmatrix}$$





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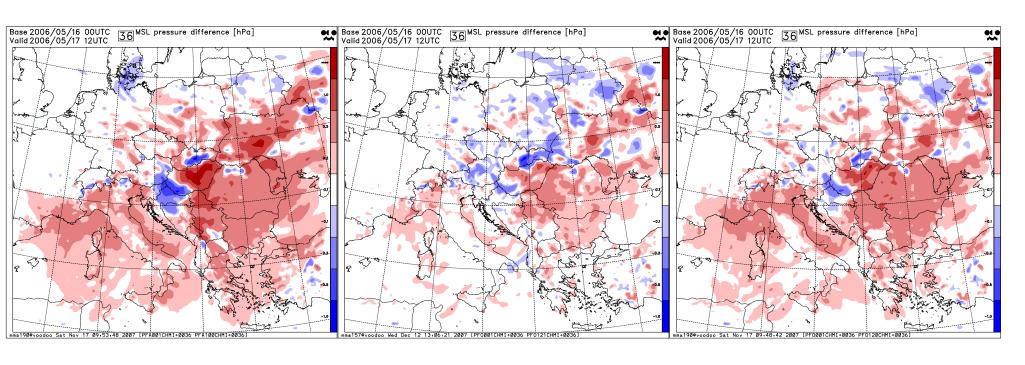
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The implementation distinguish between  $\varepsilon_H$  and  $\varepsilon_V$ 





### Impact of SLHD to MSL pressure bias



old SLHD

new SLHD

new SLHD;  $\varepsilon_V = 0.02$ 

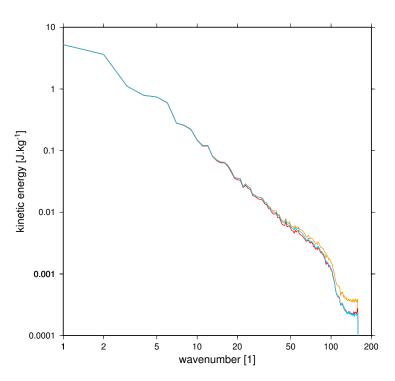




#### Impact to KE spectra

Impact of gridpoint part of SLHD (kinetic energy spectra, level 041, t = +0006 h)

Impact of gridpoint part of SLHD (kinetic energy spectra, level 041, t = +0006 h)



gridpoint part of SLHD, lag gridpoint part of SLHD, (1- $\kappa$ ).lag +  $\kappa$ .quad (-2 <  $\kappa$  < 6),  $\epsilon_H$  = 0.02 gridpoint part of SLHD, (1- $\kappa$ ).lag +  $\kappa$ .quad (0 <  $\kappa$  < 6),  $\epsilon_H$  = 0

nwp central europe

gridpoint part of SLHD, lag gridpoint part of SLHD, lag\_s,  $\epsilon_{H}$  = 0.05,  $\epsilon_{V}$  = 0 gridpoint part of SLHD, lag\_s,  $\epsilon_{H}$  = 0.05,  $\epsilon_{V}$  = 0.05

5

10

wavenumber [1]

kinetic energy [J.kg<sup>-1</sup>]

0.1

0.01

0.001

0.0001

2

50

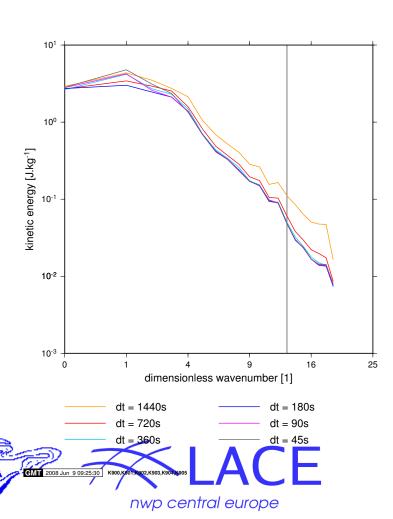
100

20

### Impact of $\Delta t$

Kinetic energy spectrum

(+0006 hour forecast, model level 041)

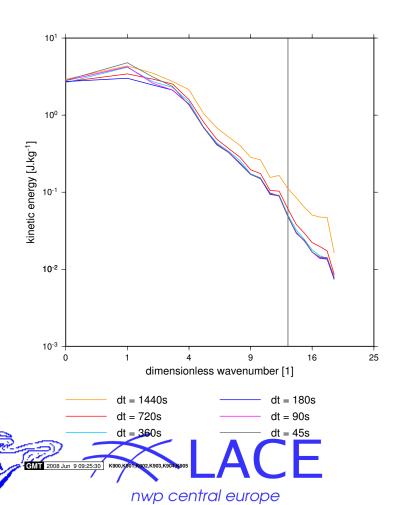


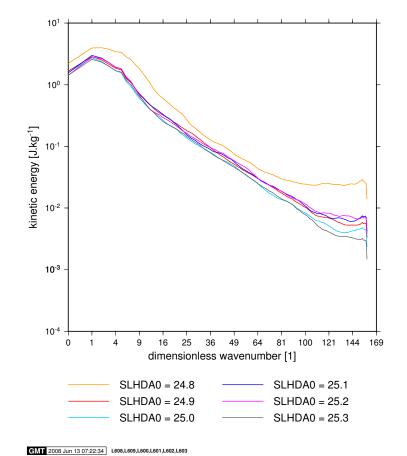
#### Impact of $\Delta t$

Kinetic energy spectrum

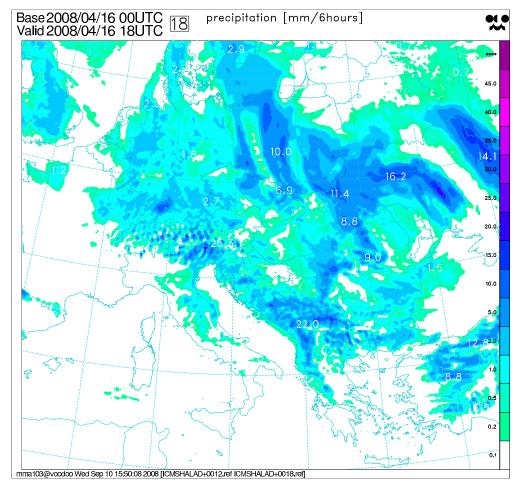
(+0006 hour forecast, model level 041)

Sensitivity of kinetic energy spectrum to SLHDA0 (+0006h forecast, model level 041, dx = 2.5km, lag + quad, NITMP = 2)





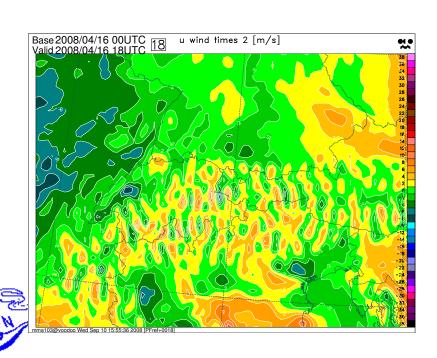
Work of: F. Váňa and R. Brožková (Cz)



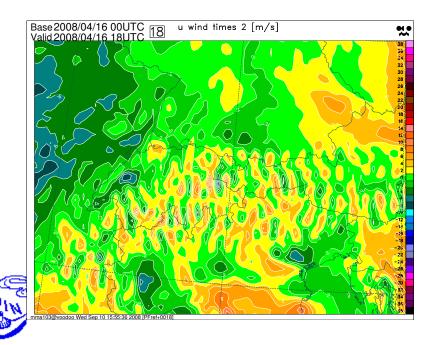


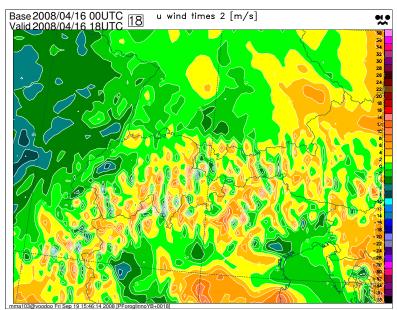


 Quadratic orography modified according Bouteloup (MWR, 1995)

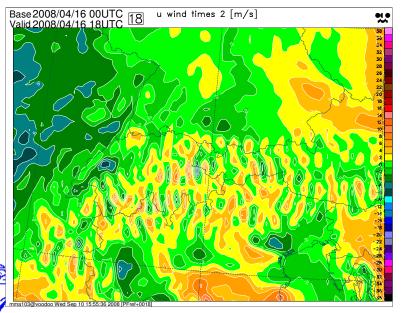


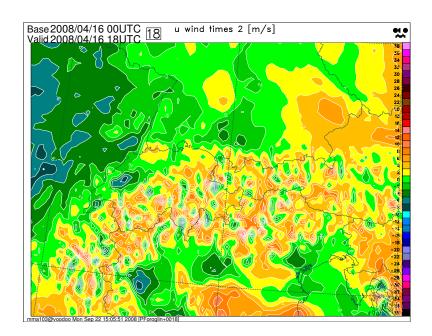
- Quadratic orography modified according Bouteloup (MWR, 1995)
- Linear orography filtered by diffusion operator



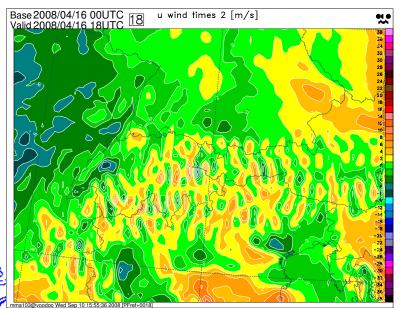


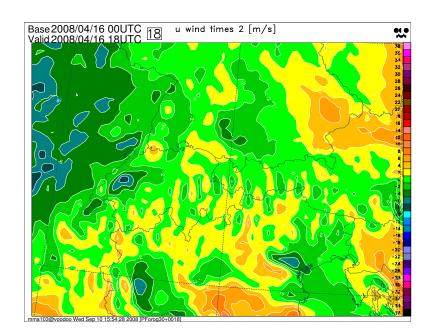
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- Linear orography, no filtering
- Quadratic orography, no filtering
- ⇒ A new cost function formulation ought to be defined. The E-zone seems to be an attractive place to displace the "noise" from model flat areas.



## Other topics

Implementation of the fully compressible flux conservative thermodynamic equations Work of: P. Smolíková and R. Brožková (Cz)



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- Implementation of the fully compressible flux conservative thermodynamic equations Work of: P. Smolíková and R. Brožková (Cz)
- Interaction of DFI with the way how the derivatives of RT are computed

Work of: P. Smolíková and R. Brožková (Cz)

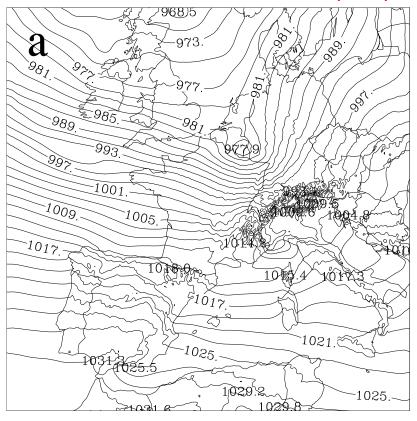


## Other topics

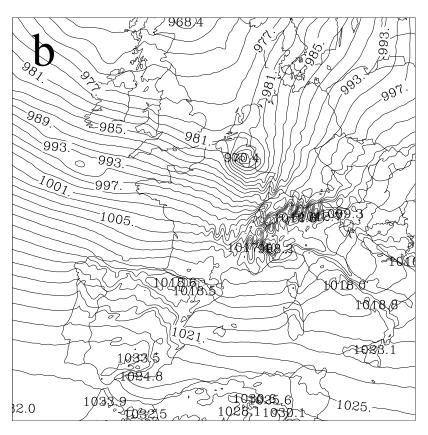
- Implementation of the fully compressible flux conservative thermodynamic equations Work of: P. Smolíková and R. Brožková (Cz)
- Interaction of DFI with the way how the derivatives of RT are computed Work of: P. Smolíková and R. Brožková (Cz)
- 2<sup>nd</sup> order accurate physics-dynamics interface Work of: I. Bašták-Durán (Sk), P. Termonia and R. Hamdi (Be)



#### Work of: P. Termonia (Be)



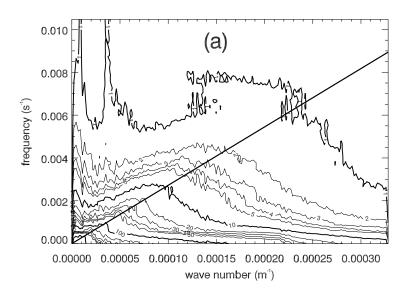
The result of a standard (operationally) used DFI (977.9 hPa).



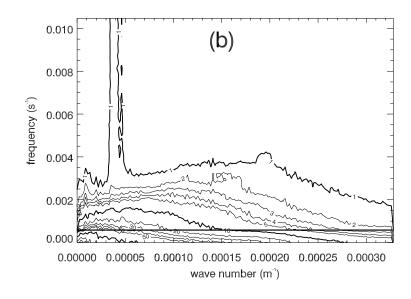
ALADIN forecast after developing for 9 h (970.4 hPa).



### Spectrum in time and space



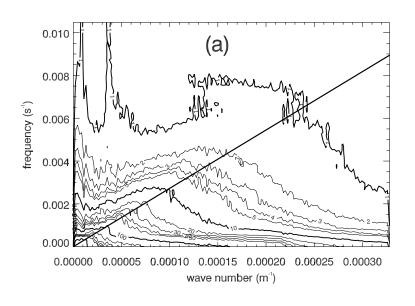
The Lothar storm  $\ln p_s$  decomposed between 0600 UTC and 1200 UTC on 28 December 1999. The thick line is the propagation speed of the storm in this time interval: 98 km/h.

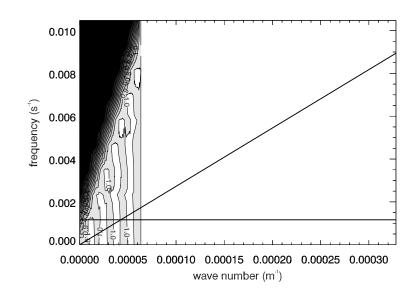


 $\ln p_s$  decomposed between 0600 UTC and 1200 UTC of an anticyclonic case on 28 December 1999. The thick horizontal line corresponds to a filter cut-off period of 3 h.



### Scale-selective low-pass windows





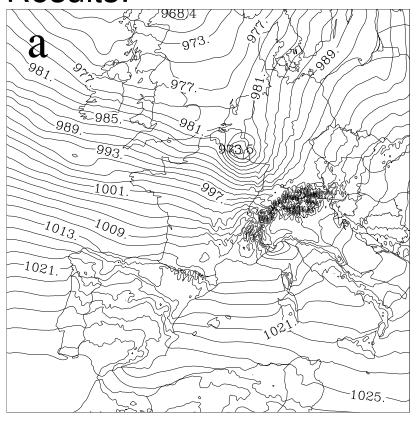
The scale-selective cut-off frequency of a low-pass Lancsoz filter:

$$\omega_c(\kappa) = \begin{cases} \omega_c^0 + \frac{\kappa}{\kappa_c} \left( \frac{\pi}{\Delta t} - \omega_c^0 \right) & \text{if} \quad \kappa \le \kappa_c \\ \frac{\pi}{\Delta t} & \text{if} \quad \kappa > \kappa_c \end{cases}$$

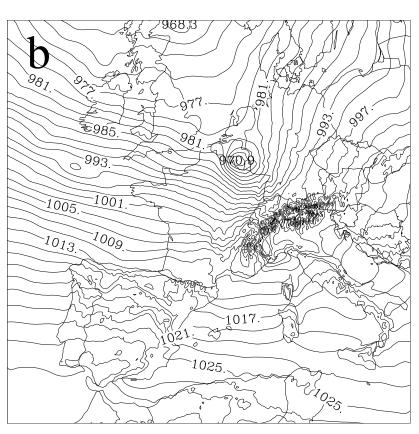
The cut-off period is  $T_c^0=2\pi/\omega_c^0$  while the *slope* of the cut-off frequencies is  $c=\pi/(\kappa_c\Delta t)$ .



#### Results:



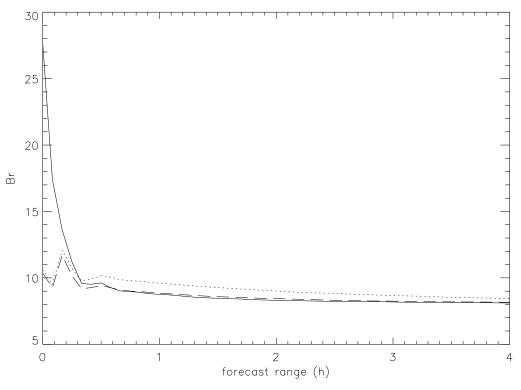
a run with  $T_c^0 = 3h$  (973.5 hPa).



a run with  $T_c^0 = 1.5 h$  (970.9 hPa).



$$Br=100\,rac{\sum_{IJ}\left|\sum_{L}
abla\cdot\Delta p_{L}\mathbf{V}_{IJL}\right|}{\sum_{IJ}\sum_{L}\left|
abla\cdot\Delta p_{L}\mathbf{V}_{IJL}\right|}$$
 ( Lynch and Huang, MWR, 1992)



solid: uninitialized

dots: full DFI

dashed: SSDFI<sub>1.5h</sub>

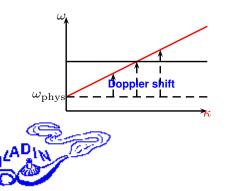
There are 2 surprises:

- filtering *less*  $(SSDFI_{1.5h}) \Rightarrow \textit{more}$ balanced!
- but, full DFI is worse than uninitialized after half and hour!?

DFI actually creates an unbalance in the *slow* part of the part of dynamics! So it needs a longer time to adjust.

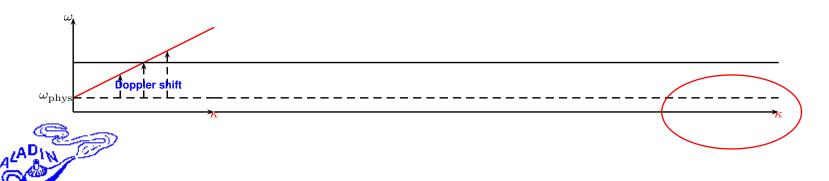


### Going to higher resolution

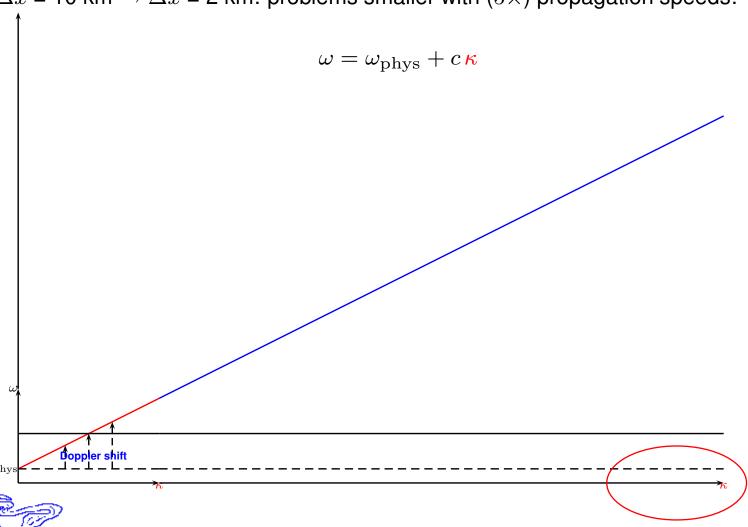


### Going to higher resolution

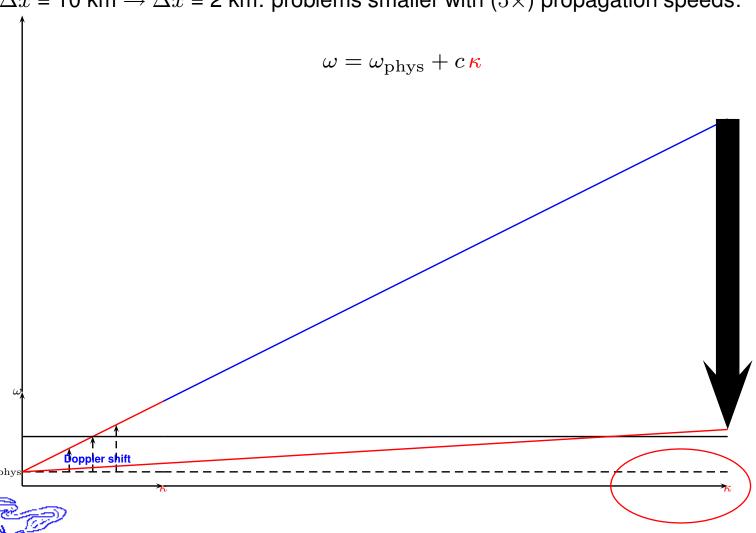
$$\omega = \omega_{\rm phys} + c \kappa$$



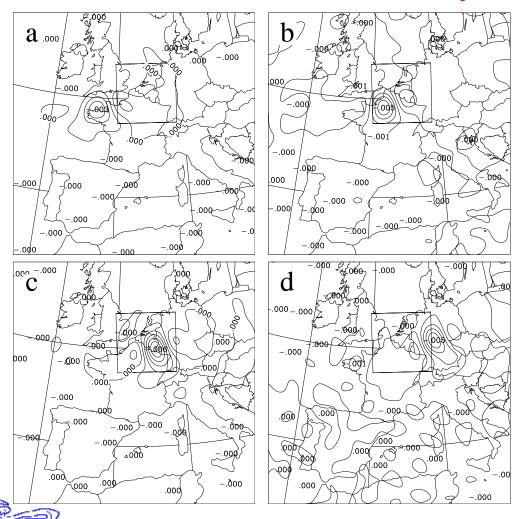
### Going to higher resolution



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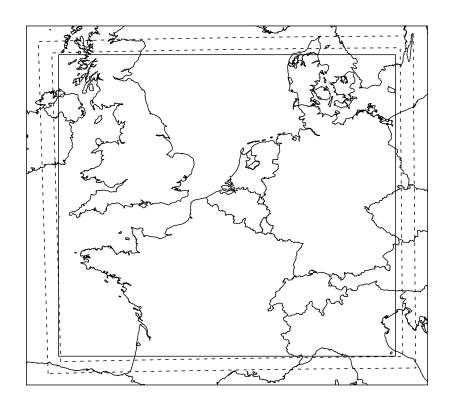


### Work of: P. Termonia, A Deckmyn and R. Hamdi (Be)



The monitoring by the MCUF field is done in ALADIN-France, i.e. the coupling model.

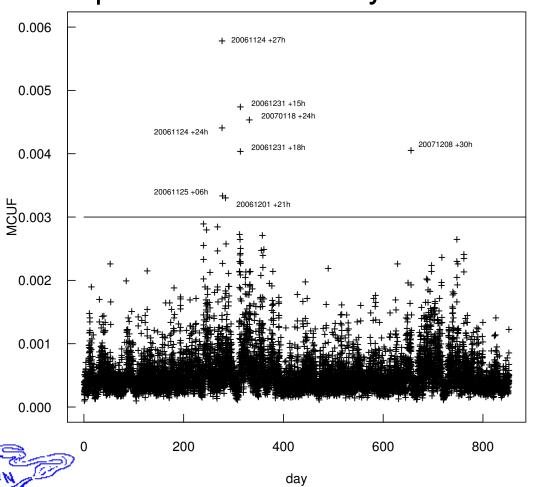
This MCUF field is operationally computed in ARPEGE and written to the coupling files of the ALADIN models. We considered it in the frame (solid line) covering the Davies zone (dashed),





#### The maximum MCUF in the frame

in the period 21 February 2006 – 30 June 2008



Let us consider a threshold value of 0.003. Then we had 8 alerts.

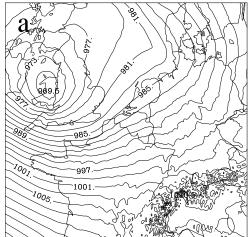
#### The maximum MCUF in the frame

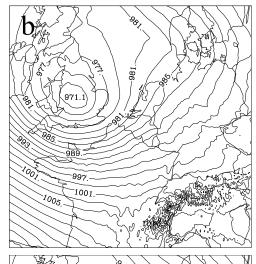
date	MCUF time	MCUF value	type	BER time
2006/11/24	+24h	0.0044	incoming	+27 h
	+27h	0.0058	incoming	+27 h
2006/11/25	+06h	0.0033	incoming	+09 h
2006/12/01	+21h	0.0033	corner (NE)	+24 h
2006/12/31	+15h	0.0047	tangent	+18 h
	+18h	0.0040	tangent	+18 h
2007/01/18	+24h	0.0045	outgoing	+ 30 h
2007/12/08	+30h	0.0041	incoming	+ 33 h

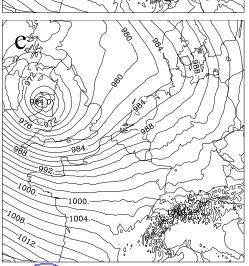
We carry out a restart 3 hours later than the MCUF alert: *Boundary-Error Restarts* (**BER**). However these restarts should be initialized by a SSDFI!!! Otherwise, we will filter out the low again in the restart in a way that is comparable to the loss at the boundary.

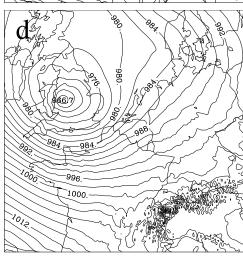


## Improvements by a restart









- (a) 33-h forecast range (969.5 hPa)
- (b) 36-h forecast range (971.1 hPa)
- (c) BER at 0900 UTC (964.0 hPa)
- (d) BER at 1200 UTC (966.7 hPa).
- $\Rightarrow$  4.4 hPa improvement.