



Dynamics & Coupling

2006-2007 progress report

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CHMI



VFE scheme for NH dynamics



Work of: **E. Larrieau Rosina (Sk)** and **J. Vivoda (Sk)**

- VFE scheme successfully implemented into the HY model (Untch and Hortal, 2004)



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- VFE scheme successfully implemented into the HY model (Untch and Hortal, 2004) \Rightarrow extension into NH dynamics with HY model as a limit case
- The only non-local operations in the vertical are integrations in HY dynamics (SL version). In NH dynamics also derivatives play crucial role (structure equation contains vertical laplacian).

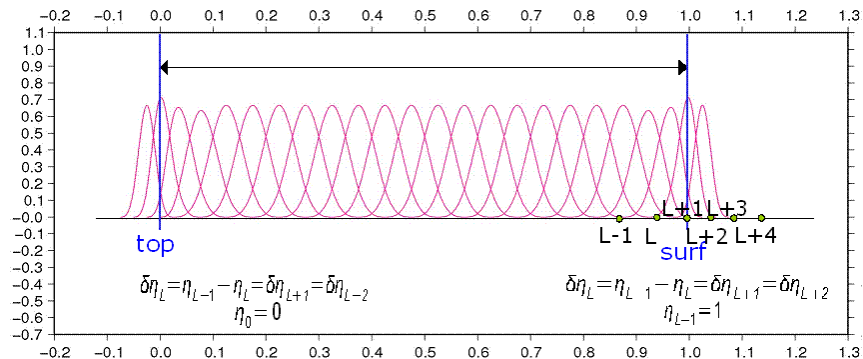


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- The only non-local operations in the vertical are integrations in HY dynamics (SL version). In NH dynamics also derivatives play crucial role (structure equation contains vertical laplacian).
- FE derivative operator based on the same basis function as used by Untch and Hortal.

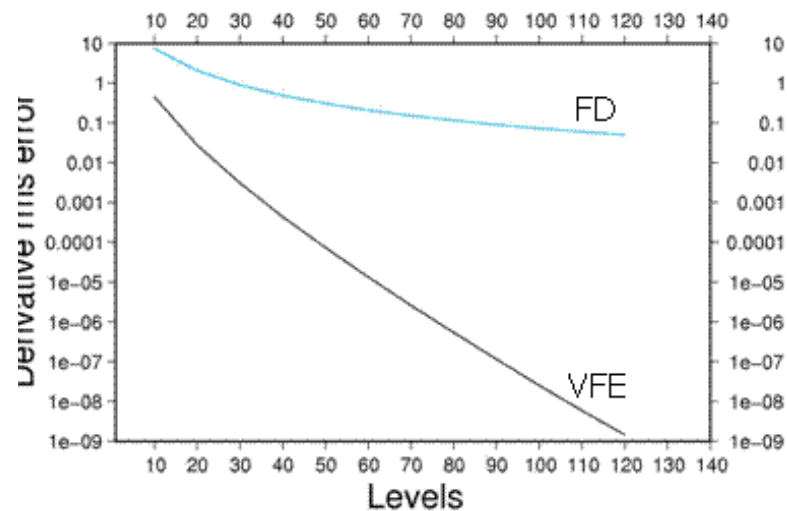
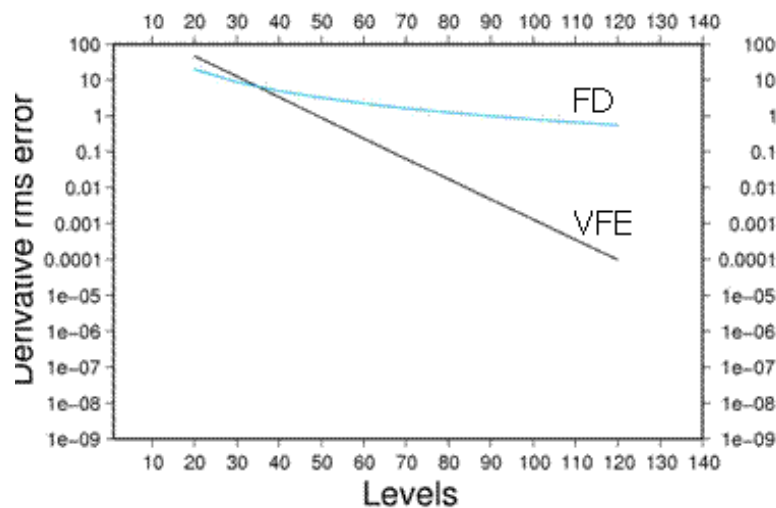


VFE scheme for NH dynamics



FE derivative operator accuracy with respect to BCs

Test function: $f(\eta) = \sin(6\pi\eta)$



$$f(\eta = 0) = f_1$$

$$f'(\eta = 0) = 0$$

$$f(\eta = 1) = f_L$$

$$f'(\eta = 1) = 0$$

$$f(\eta = 0) = \frac{\delta\eta_1 - \delta\eta_0}{\delta\eta_1} f_1 - \frac{\delta\eta_0}{\delta\eta_1} f_2$$

$$f'(\eta = 0) = \frac{f_1 - f_2}{\delta\eta_1}$$

$$f(\eta = 1) = \frac{\delta\eta_{L-1} - \delta\eta_L}{\delta\eta_{L-1}} f_L - \frac{\delta\eta_L}{\delta\eta_{L-1}} f_{L-1}$$

$$f'(\eta = 1) = \frac{f_L - f_{L-1}}{\delta\eta_{L-1}}$$



VFE scheme for NH dynamics

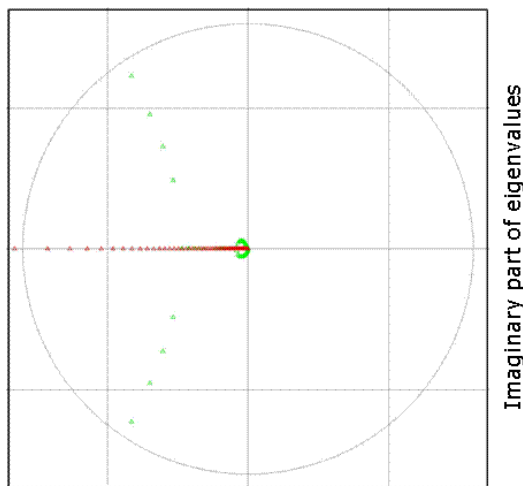


Laplacian term FE treatment

In linear and non-linear model the laplacian is explicit and has the same form (thanks to fact that the vertical divergence related prognostic variable is used):

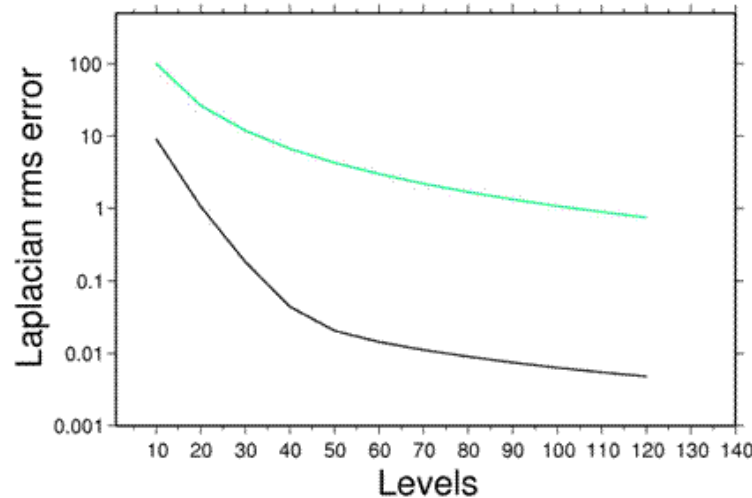
$$\text{V1: } LP = \frac{\pi}{m} \frac{\partial}{\partial \eta} \left(\frac{1}{m} \frac{\partial \pi P}{\partial \eta} \right) \quad \text{V2: } LP = \frac{\pi}{m} \frac{\partial}{\partial \eta} \left(\frac{\pi^2}{m} \right) \frac{\partial P}{\partial \eta} + \left(\frac{\pi}{m} \right)^2 \frac{\partial}{\partial \eta} \left(\frac{\partial P}{\partial \eta} \right)$$

boundary conditions the same as in FD



Imaginary part of eigenvalues

Real part of eigenvalues

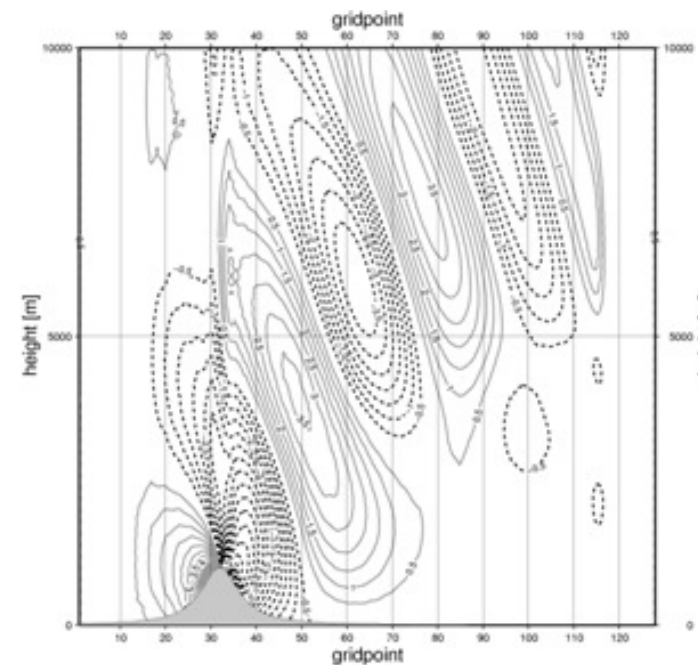
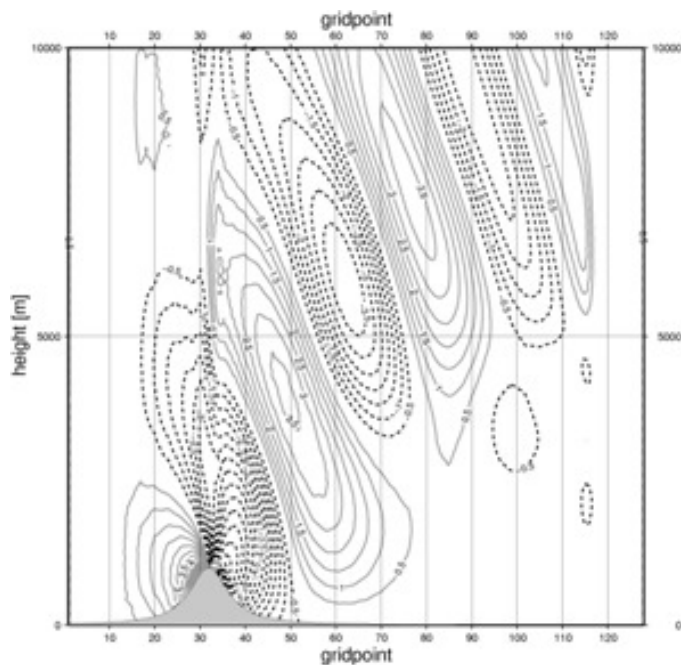


VFE scheme for NH dynamics



Constraints

- C1 constraint allows to have one structure equation for the solver. Otherwise solver becomes of $2L \times 2L$ kind to be solved iteratively (extra 30% of CPU).



VFE scheme for NH dynamics



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- C2 constraint defines stability requirements. (Even in case of C1 is not satisfied, C2 is required assuming that C1 is almost satisfied.)



VFE scheme for NH dynamics



Constraints

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- C2 constraint defines stability requirements. (Even in case of C1 is not satisfied, C2 is required assuming that C1 is almost satisfied.)
- Stability properties are equivalent to those of FD model



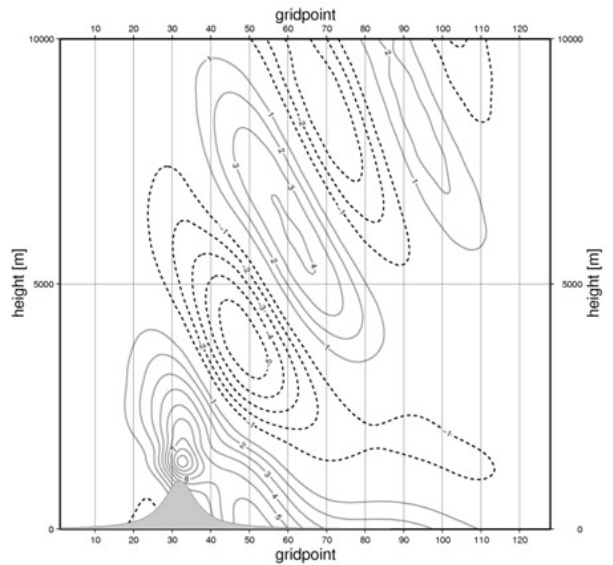
VFE scheme for NH dynamics



Non-linear model discretization

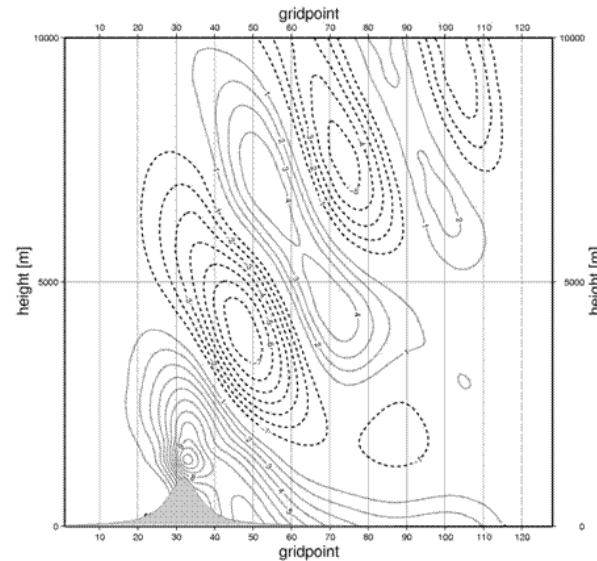
$$\text{Z-term: } Z = \frac{p}{mRT} \nabla gw \frac{\partial \vec{V}}{\partial \eta}$$

$$\text{X-term: } X = \frac{p}{mRT} \nabla \Phi \frac{\partial \vec{V}}{\partial \eta}$$



167 2008 Nov 30 16:36:42 experiment: VF19

min: -5.7843
max: 9.6362
step: 1



167 2008 Nov 30 20:30:34 experiment: VF19

min: -7.6637
max: 11.46
step: 1

VFE (X-term FD)

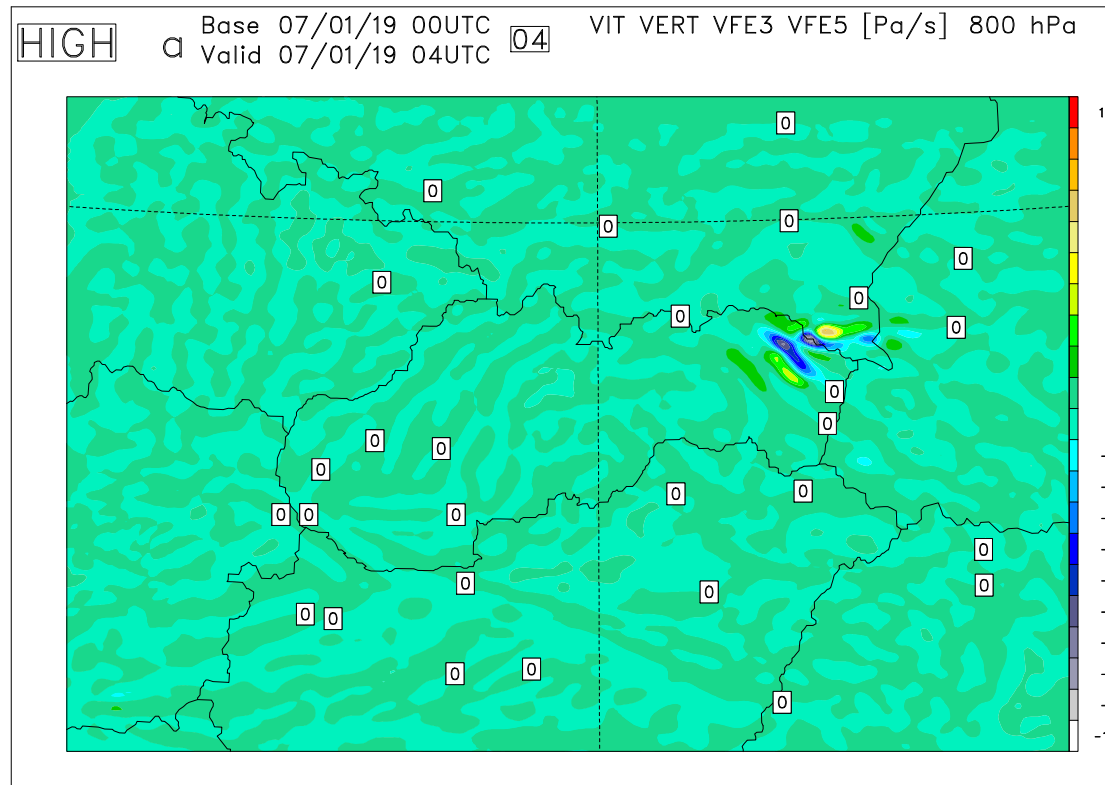
VFE(Z-term FD)



VFE scheme for NH dynamics



Non linear terms on 3D tests:



VFE (integral and laplacian only) - VFE (... + X-term)



VFE scheme for NH dynamics



Conclusions

- Analysis of stability in linear framework suggests that HY VFE extension to NH VFE is possible.



VFE scheme for NH dynamics



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- From stability point of view the crucial is the definition of vertical laplacian operator (eigenvalues must be real and negative).



VFE scheme for NH dynamics



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- Spectral solver is made iterative, the convergence is very fast.



VFE scheme for NH dynamics



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- The scheme is stable (3D tests with $\Delta x = 2.5$ km, $\Delta t = 120$ s).



VFE scheme for NH dynamics



Conclusions

- Analysis of stability in linear framework suggests that HY VFE extension to NH VFE is possible.
- From stability point of view the crucial is the definition of vertical laplacian operator (eigenvalues must be real and negative).
- Spectral solver is made iterative, the convergence is very fast.
- The scheme is stable (3D tests with $\Delta x = 2.5$ km, $\Delta t = 120$ s).
- The BCs for non-linear terms are source of noise.



New interpolators for SL

Work of: J. Mašek (Sk) and F. Váňa (Cz)

Family of two parametric cubic interpolators

$$\begin{aligned} F(\mathbf{x}, \mathbf{y}) = & w_0(\mathbf{x})y_0 + w_1(\mathbf{x})y_1 \\ & + w_1(1 - \mathbf{x})y_2 + w_0(1 - \mathbf{x})y_3 \end{aligned}$$

where

$$w_0(\mathbf{x}) = a_1\mathbf{x} + a_2\mathbf{x}^2 - (a_1 + a_2)\mathbf{x}^3$$

$$w_1(\mathbf{x}) = 1 + (a_2 - 1)\mathbf{x} - (3a_1 + 4a_2)\mathbf{x}^2 + 3(a_1 + a_2)\mathbf{x}^3$$



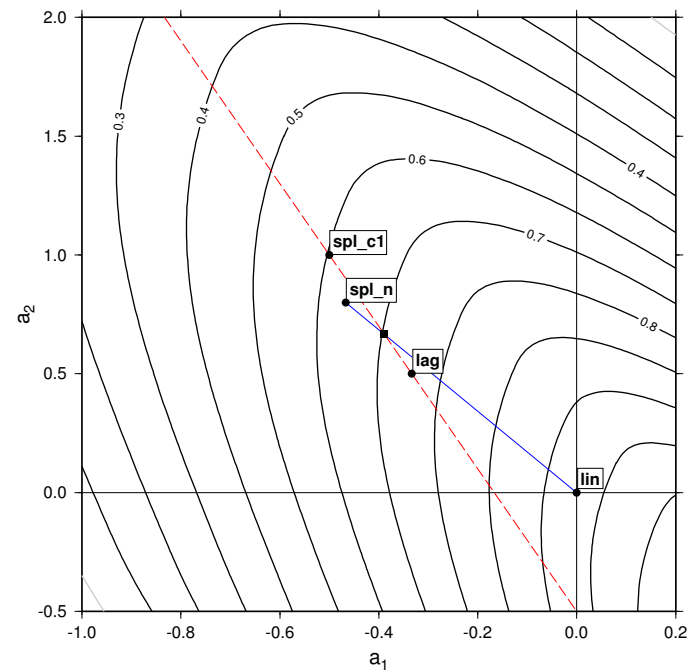
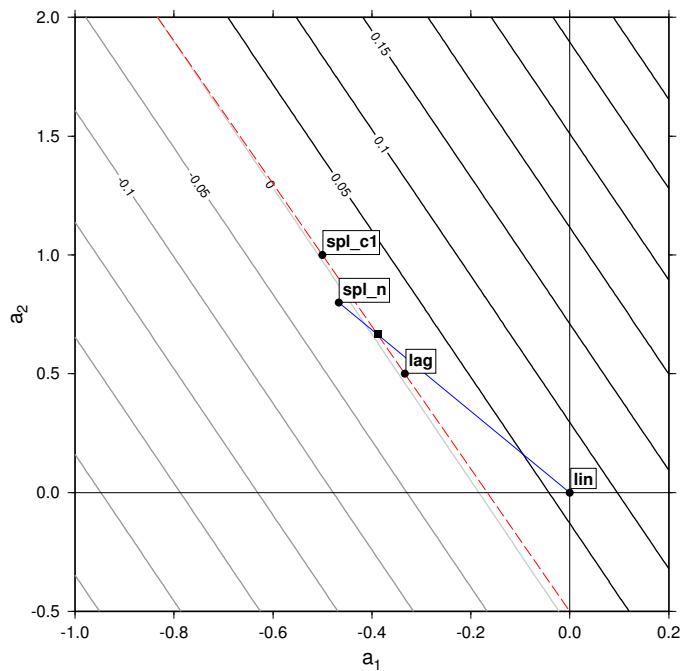


New interpolators for SL

Dimensionless damping rate

Damping factor for $N = 100, m = 10$

Damping factor for $N = 100, m = 40$





New interpolators for SL

New (SLHD) time-step organization

original data-flow

new data-flow



New interpolators for SL



New (SLHD) time-step organization

original data-flow

new data-flow

Step 1

computation of weights for

A_1, A_L

computation of all weights:

$$A = A_1 + \kappa (A_2 - A_1)$$



New interpolators for SL



New (SLHD) time-step organization

original data-flow

new data-flow

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computation of all weights:
 $A = A_1 + \kappa (A_2 - A_1)$

Step 2

high order (A_1) interpolation

all (A) interpolation



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diffusive interpolation by
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-





New interpolators for SL

New (SLHD) time-step organization

original data-flow

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Step 1

computation of weights for
 A_1, A_L

computation of all weights:
 $A = A_1 + \kappa (A_2 - A_1)$

Step 2

high order (A_1) interpolation

all (A) interpolation

Step 3

diffusive interpolation by
using A_L weights

-

Step 4

combination of high order and
diffusive interpolation according κ

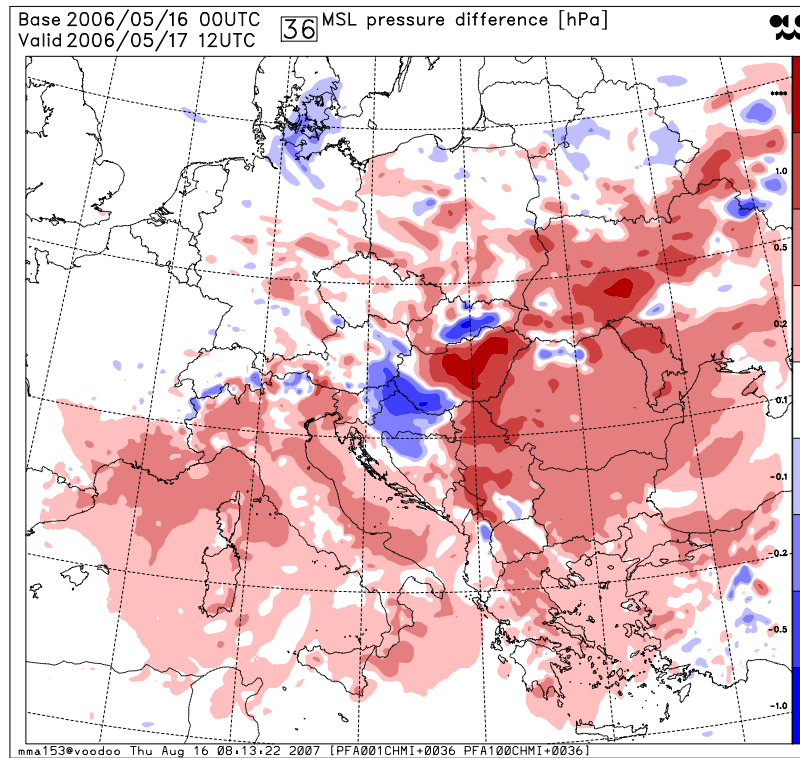
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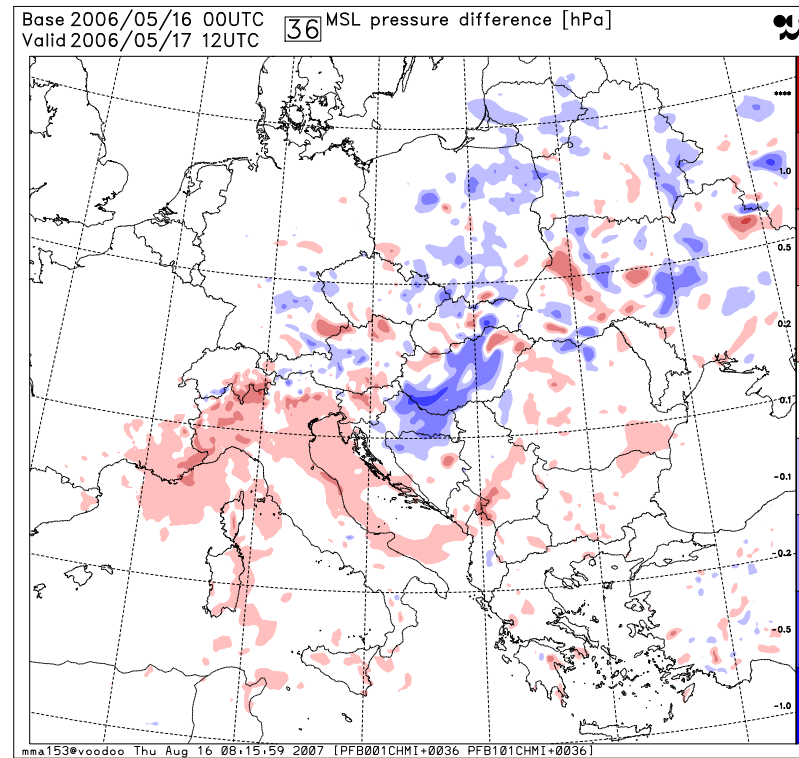


New interpolators for SL

MSL pressure differences SLHD vs. spec. diffusion



original



new



New interpolators for SL

Conclusions

- More freedom to SL interpolation.



New interpolators for SL



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- SLHD becomes just “a special case” of standard interpolation \Rightarrow TL/AD of SL can be easily adapted to TL/AD of SLHD.



New interpolators for SL



Conclusions

- More freedom to SL interpolation.
- SLHD becomes just “a special case” of standard interpolation \Rightarrow TL/AD of SL can be easily adapted to TL/AD of SLHD.
- Algorithmically more efficient (SLHD = extra 2% of CPU).



TL/AD of LAM SL



Work of: **F. Váňa (Cz)**

- Ready since January 2007 (available since April 2007)



TL/AD of LAM SL



Work of: **F. Váňa (Cz)**

- Ready since January 2007 (available since April 2007)
- More efficient and more accurate

Eulerian advection (1 hour, $\Delta t = 120$ s)

ADJOINT TEST: THE DIFFERENCE IS **10.395** TIMES THE ZERO OF THE MACHINE

SL advection (1 hour, $\Delta t = 120$ s)

ADJOINT TEST: THE DIFFERENCE IS **16.562** TIMES THE ZERO OF THE MACHINE

SL advection (1 hour, $\Delta t = 360$ s)

ADJOINT TEST: THE DIFFERENCE IS **5.452** TIMES THE ZERO OF THE MACHINE



TL/AD of LAM SL



Specific development related to vectorization in AD

Global update of all interpolations:

```
!cdir nodep
DO JINC=ISTART,ISTOP
  PSLBUF1( INC(JINC,JROF) ) = &
    & PSLBUF1( INC(JINC,JROF) ) + ZINC(JINC,JROF)
ENDDO
```



TL/AD of LAM SL



Specific development related to vectorization in AD

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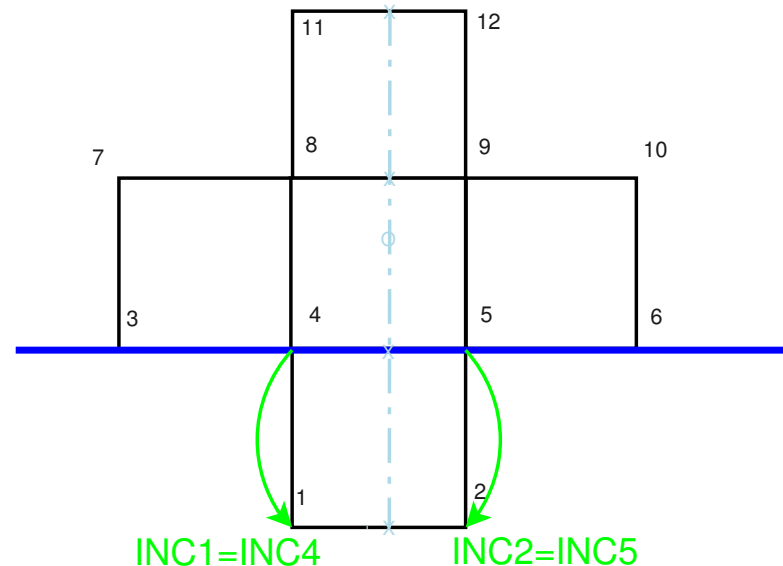
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```
ENDDO
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TL/AD of LAM SL



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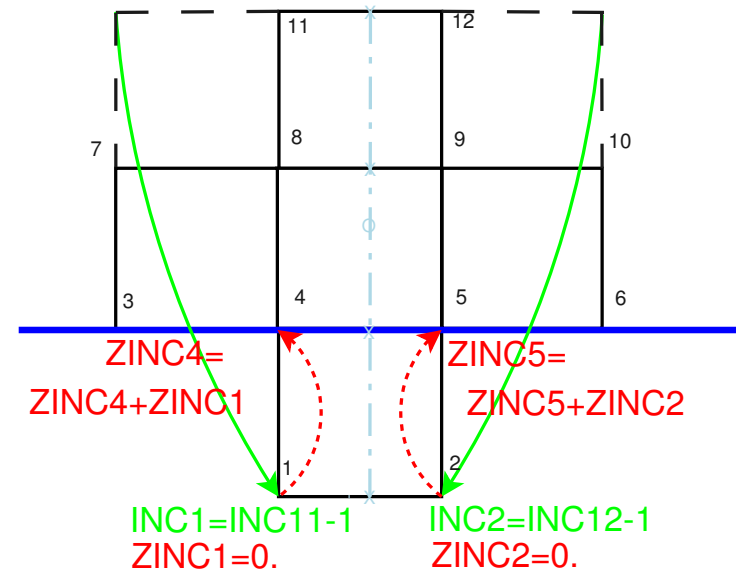
```
!cdir nodep
```

```
DO JINC=ISTART,ISTOP
```

```
  PSLBUF1 (INC (JINC, JROF' ) ) = &
```

```
    & PSLBUF1 (INC (JINC, JROF' ) ) + ZINC (JINC, JROF' )
```

```
ENDDO
```



TL/AD of LAM SL



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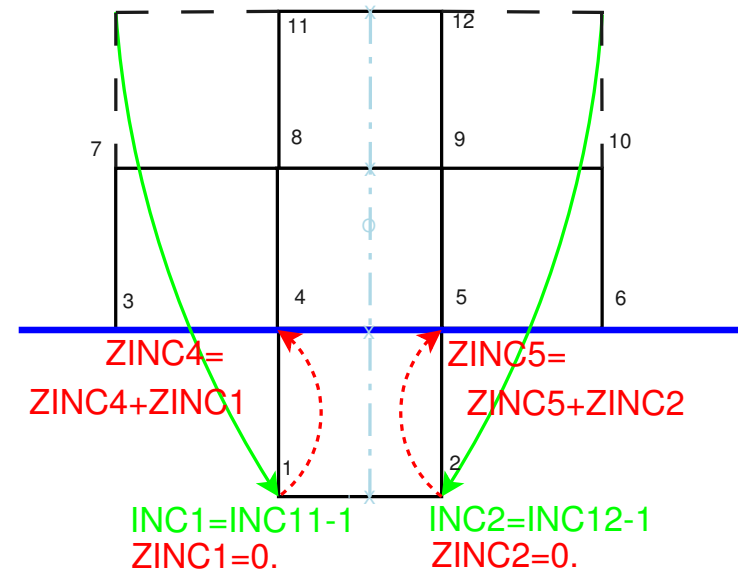
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```

```
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```

```
ENDDO
```

V.Op.Ratio = 98.814048 %

VLEN = 225.948825



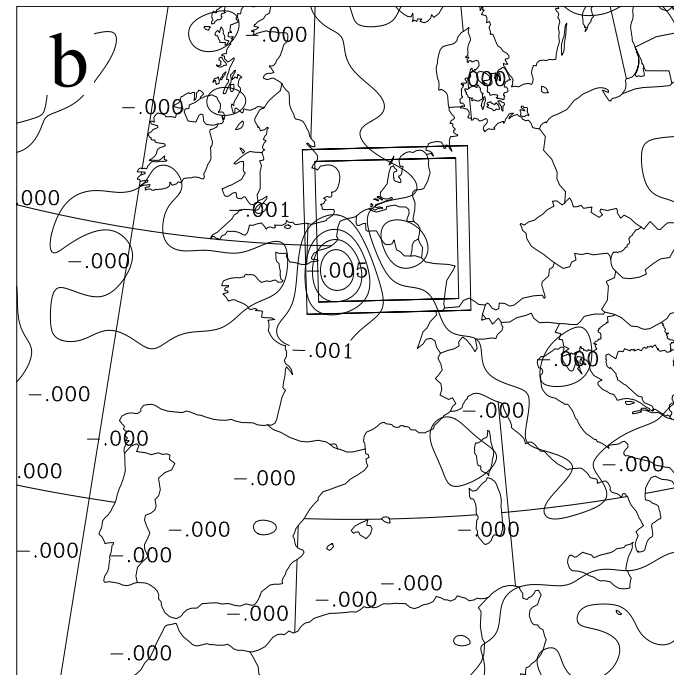
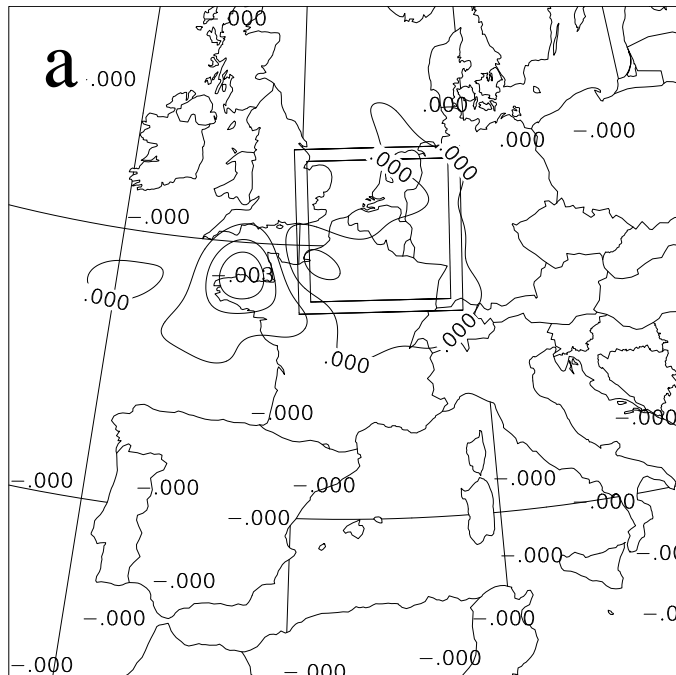
MCUF



Work of: **P. Termonia (Be)** and **A. Deckmyn (Be)**

Monitoring the Coupling-Update Frequency

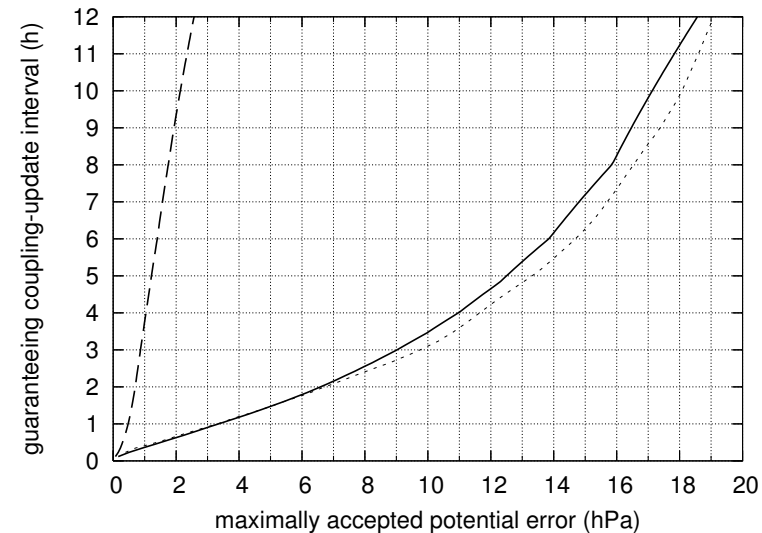
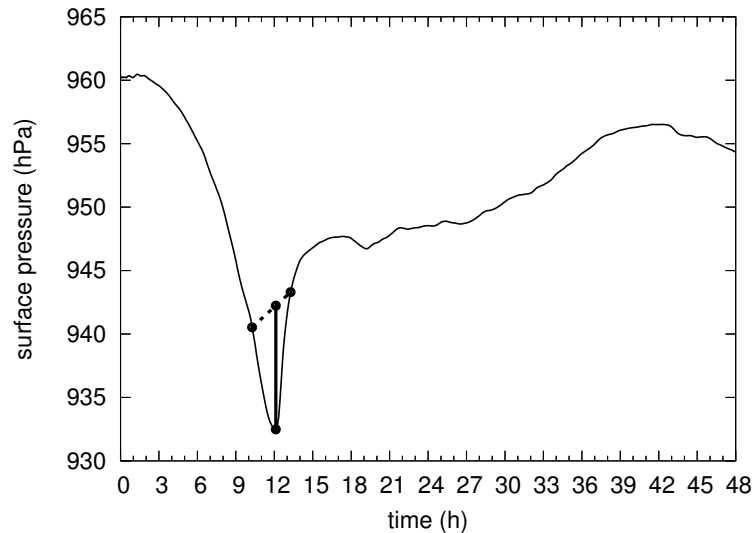
Termonia (2004), *Mon. Wea. Rev.*



This field is now present in the coupling files for ALADIN: CUF1PRESSURE!



MCUF



We need coupling intervals of about **20 min** to guarantee that we do not make interpolation errors bigger than 1 hPa.

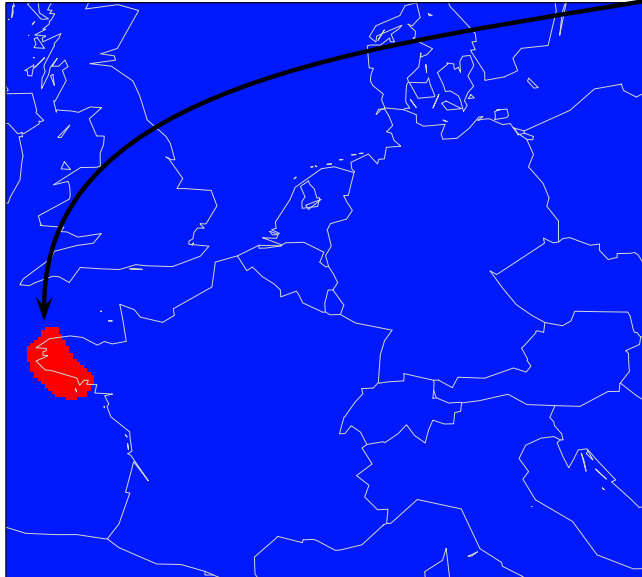
⇒ NOT feasible



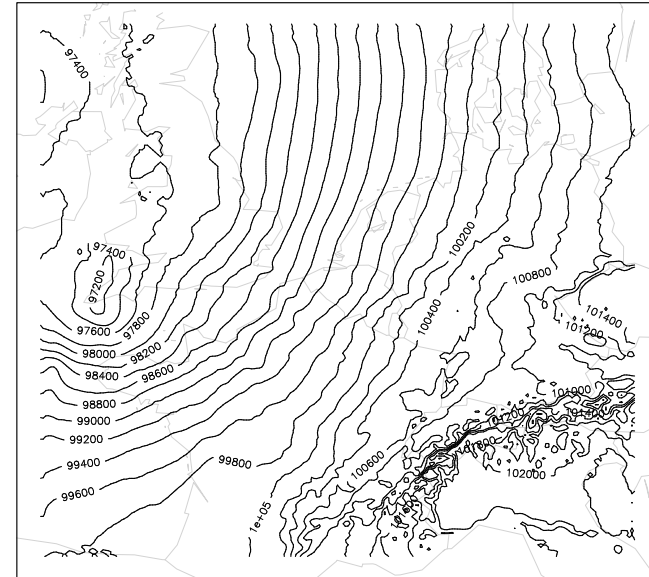
MCUF



If the CUF1PRESSURE field exceeds the threshold of 0.003 (red) then make an additional run starting from this moment, e.g. at +27 h forecast range of this run. The storm is then in the domain.



MSLPRESSURE
2006/11/24 z0:0 +27h

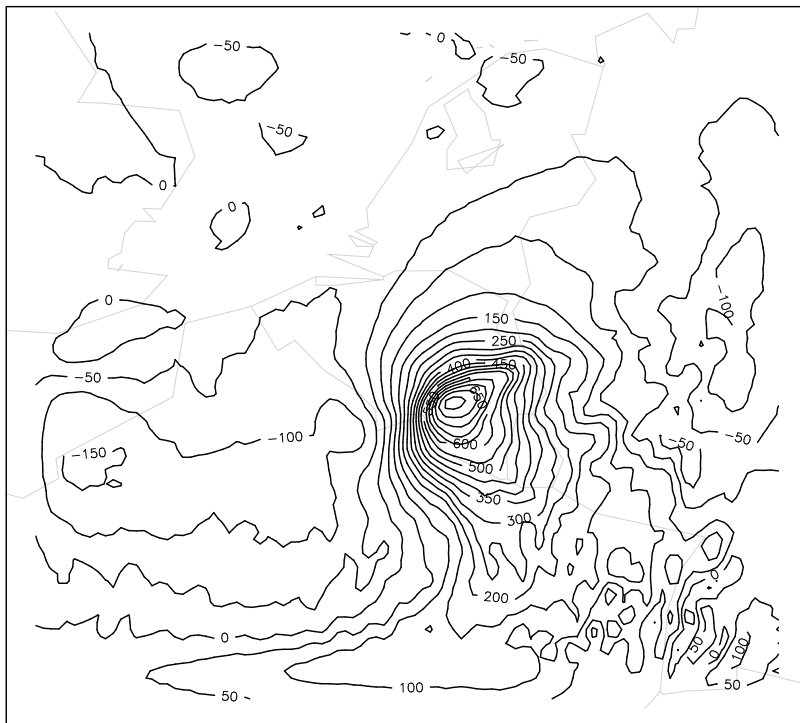




DFI filters storms !!!

However, for the later start with the storm in the domain,
DFI filters the signal of the storm:

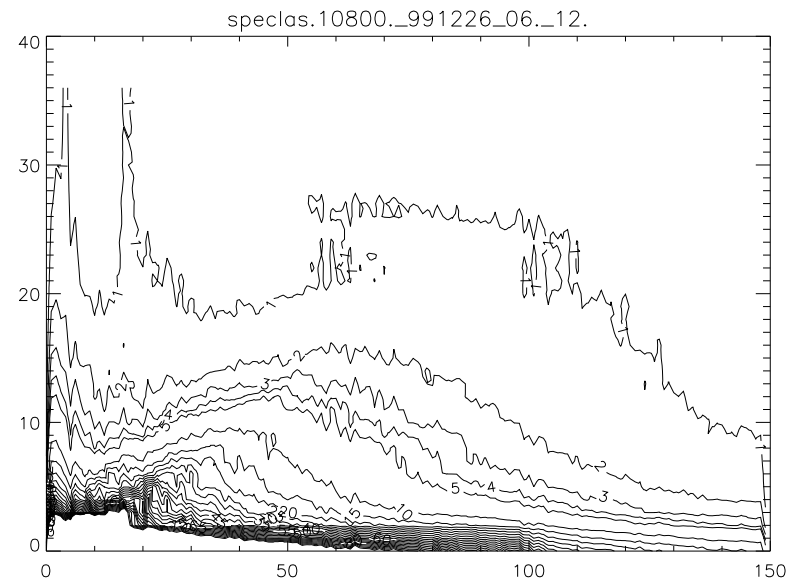
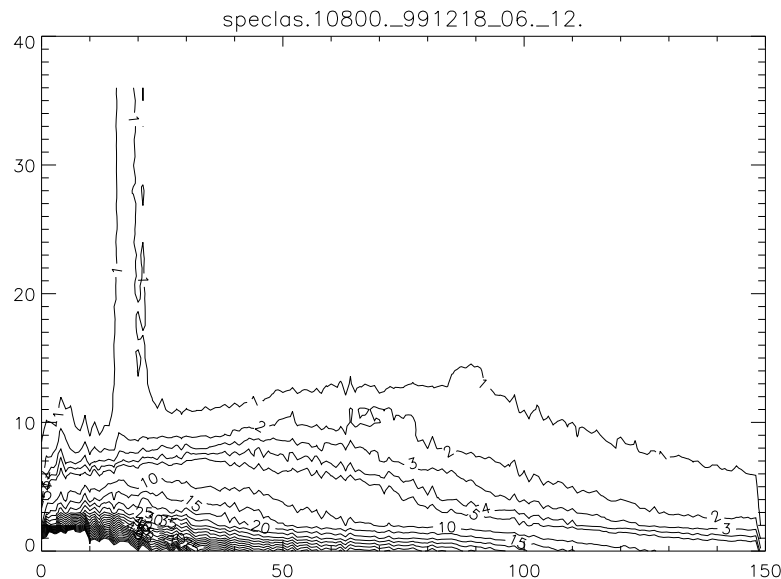
MSLP 26/12/1999 +9h
DFI(3h) – no DFI



DFI with TAUS=10800.:
max difference of about
8.5 hPa!



DFI filters storms !!!

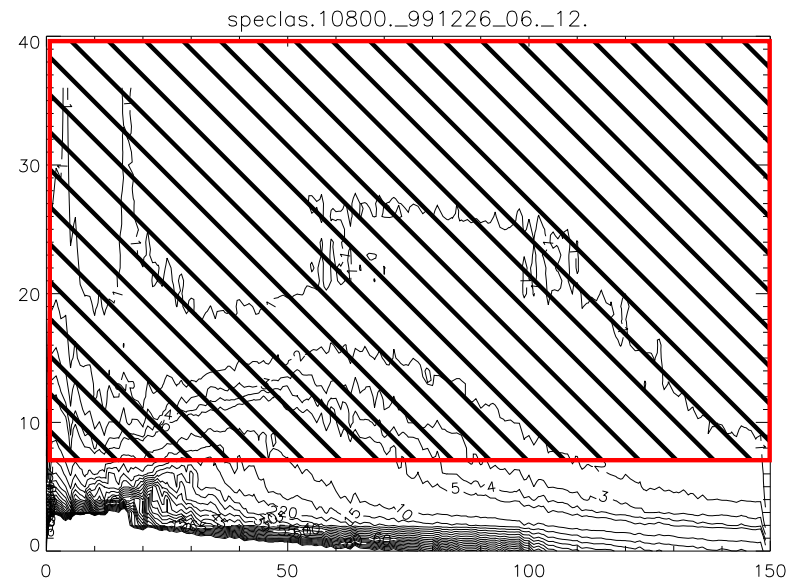
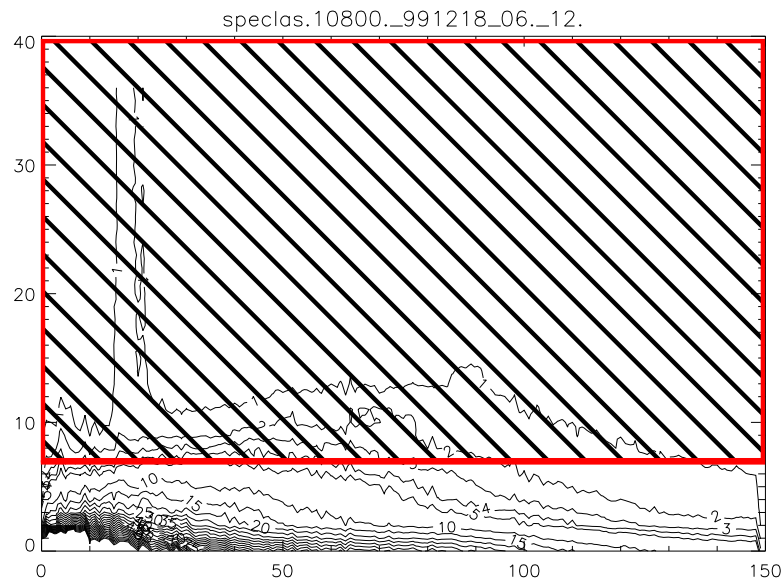


spectral decomposition in the space and time domain of a forecast without storm (left) and the Lothar storm (right).





DFI filters storms !!!

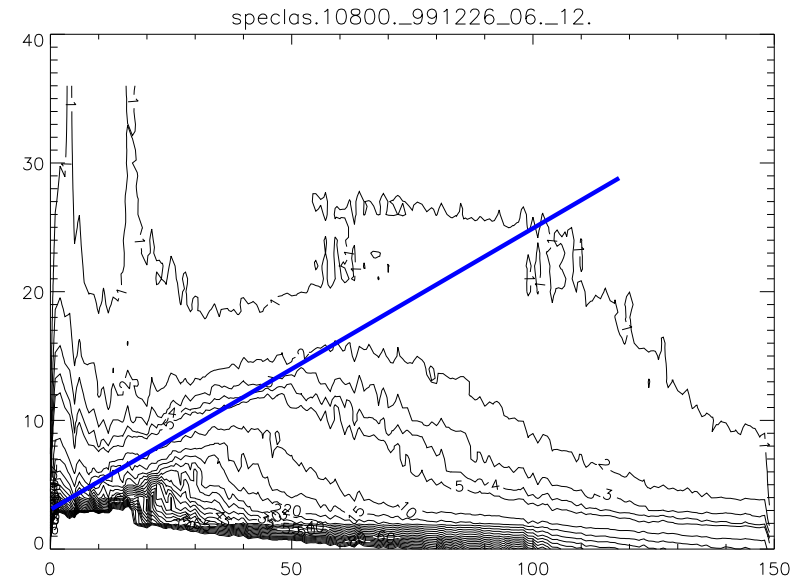
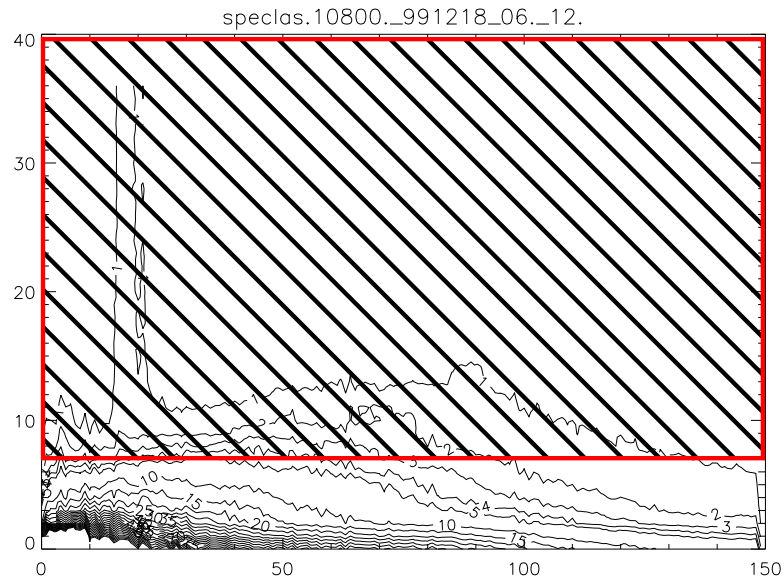


filtering





DFI filters storms !!!



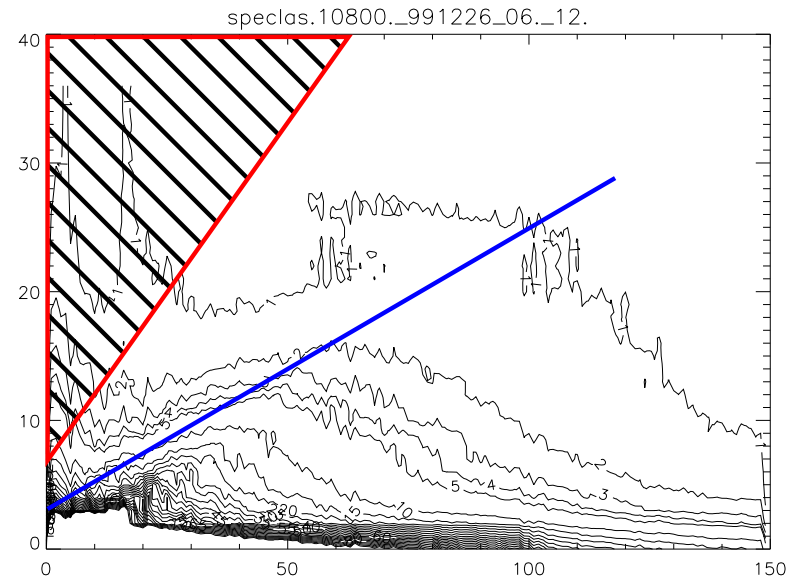
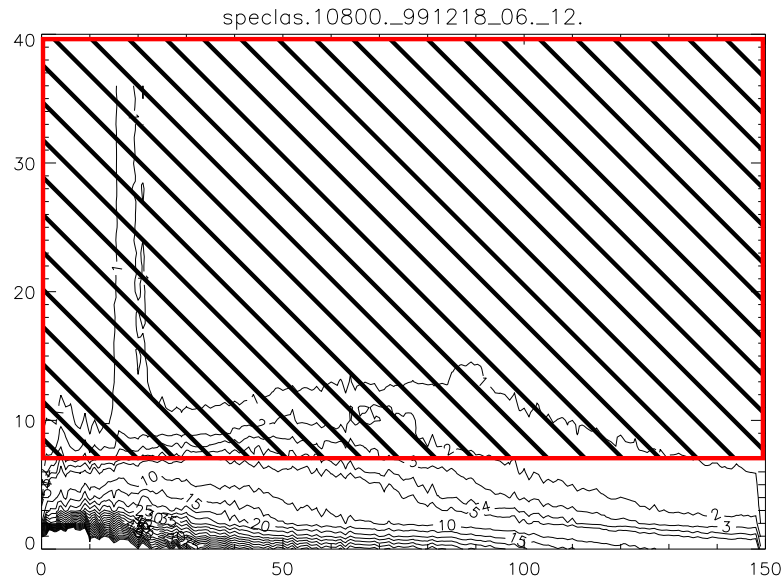
blue line corresponds to propagation speed of the Lothar storm

$$\omega/k \approx 100 \text{ km/h}$$





DFI filters storms !!!



idea: scale-selective filtering



MCUF and DFI: conclusions



- The MCUF approach can be used. The CUF1PRESSURE field is in the coupling files.



MCUF and DFI: conclusions



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MCUF and DFI: conclusions



- The MCUF approach can be used. The CUF1PRESSURE field is in the coupling files.
- In case the required CUF is too small it seems better to restart integration with the storm inside the domain
- But DFI filters storms!
- With recent ALADIN cycles the Lothar run is stable without DFI, it is possible to restart without DFI.
- Additional research needed on scale-selective DFI. Not much progress due to lack of time but planned for the future.



New approach to LBC's



Work of: **P. Termonia (Be) and F. Voitus (Fr)**

- Some alternative ideas for the Davies scheme exist where one imposes the characteristic values at the inflow LBC's and extrapolates (by upstream time differencing) the outgoing characteristics
- The work of Aidan McDonald (2000; 2003; 2005; 2006) has led to a formulation for the semi-implicit semi-Lagrangian scheme in the HIRLAM model which leads to a quality that is comparable to the Davies scheme.



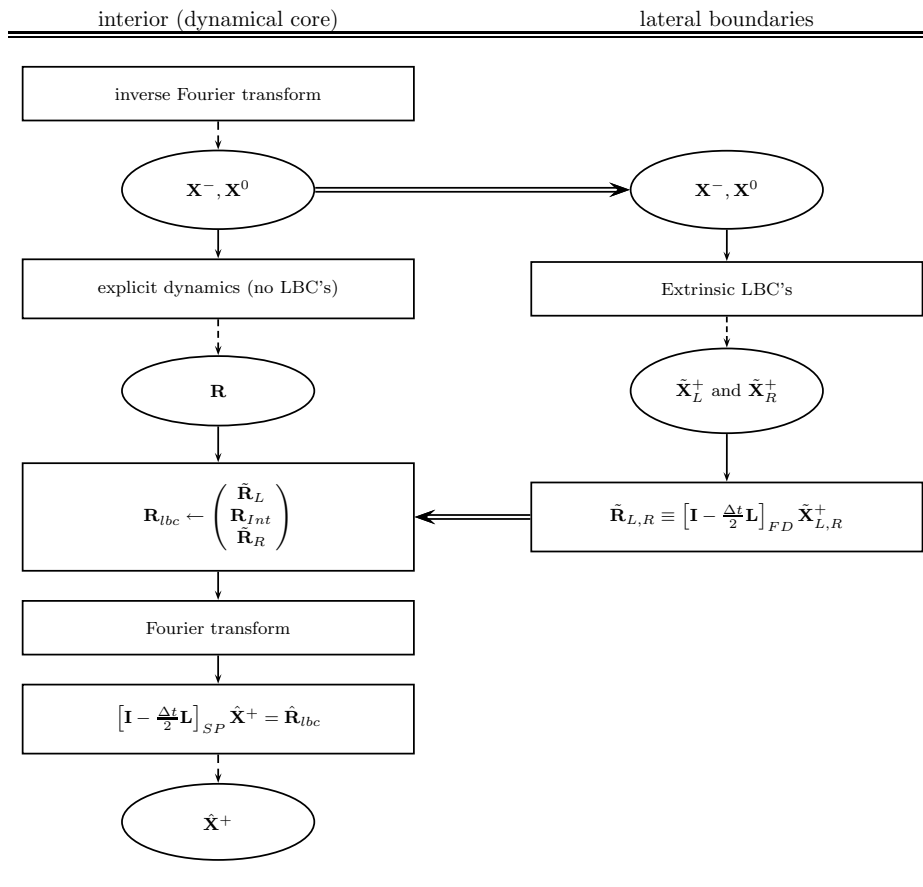
New approach to LBC's



- This is done by adapting the dynamical equations at the boundaries, i.e. in *distinct* points only.
- In order to have a stable scheme as a net result, this adaptation should be done in the implicit part of the semi-implicit scheme, in practice being the Helmholtz equation.
- In spectral models this equation is solved in spectral space where the value of a field can not be changed in distinct points!
- *Extrinsic* LBC's approach is proposed where the LBC's are computed with a numerical finite-difference scheme that is different than the SI SL scheme of the dynamical core. This can be applied in a gridpoint model but much more interestingly, it may allow to solve the problem of LBC's in spectral models ...



Extrinsic LBC's



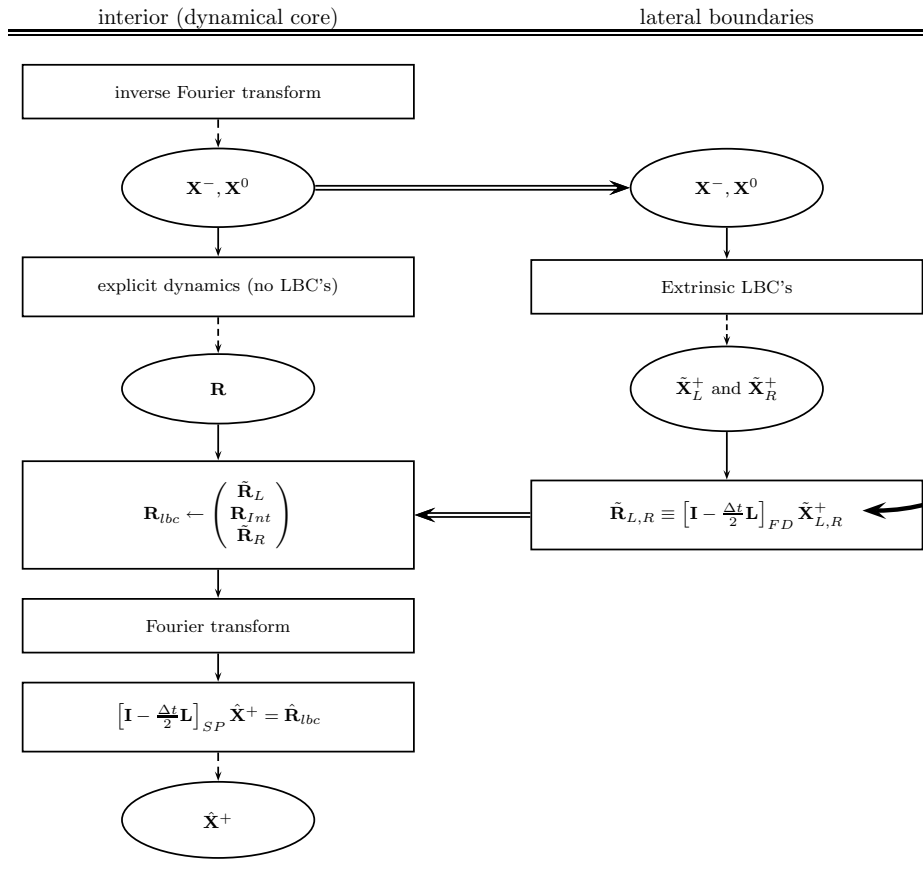
It has been shown that the result of these extrinsic schemes can be imposed at the lateral boundaries by

1. applying the implicit operator $\left[\mathbf{I} - \frac{1}{2} \Delta t \mathbf{L} \right]_{FD}$ to the result of the extrinsic LBC's in gridpoint space, and
2. overwriting the result of the explicit part \mathbf{R} of dynamics at the boundaries, before going to spectral space.





Extrinsic LBC's



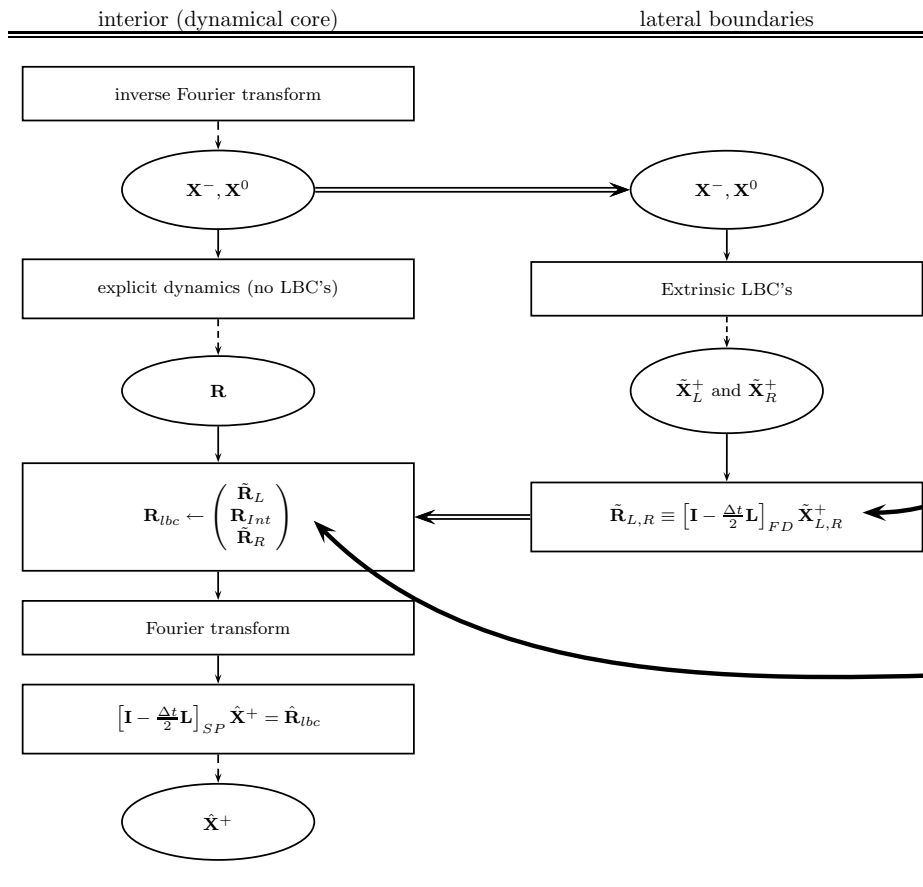
It has been shown that the result of these extrinsic schemes can be imposed at the lateral boundaries by

1. applying the implicit operator $[1 - \frac{1}{2} \Delta t \mathbf{L}]_{FD}$ to the result of the extrinsic LBC's in gridpoint space, and
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Extrinsic LBC's



It has been shown that the result of these extrinsic schemes can be imposed at the lateral boundaries by

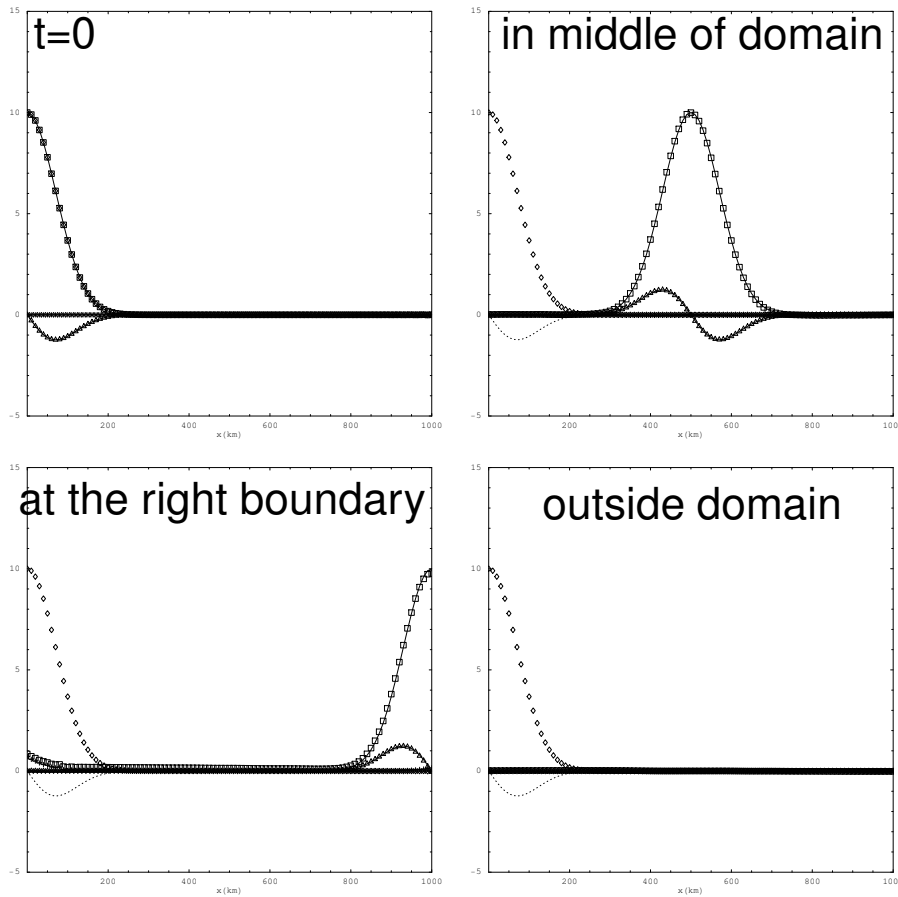
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2. overwriting the result of the explicit part R of dynamics at the boundaries, before going to spectral space.





Tests in 1D shallow water

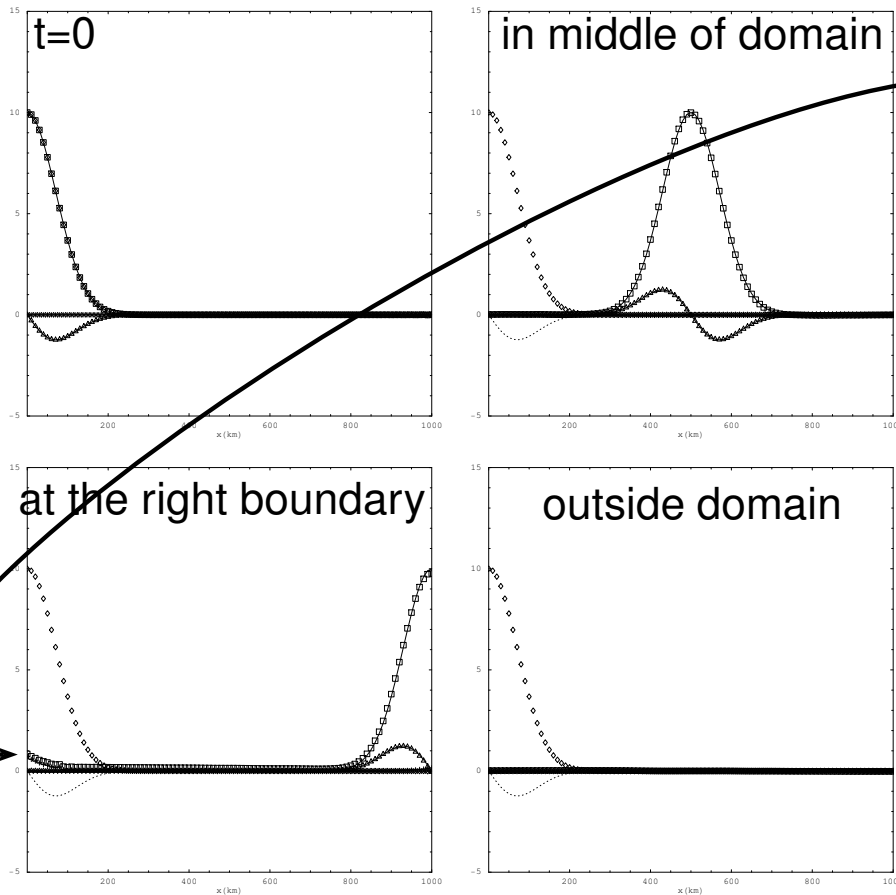
Bell-shaped feature passing the domain



Tests in 1D shallow water



Bell-shaped feature passing the domain



Inaccuracy due to inconsistency between the operator $[1 - \frac{1}{2}\Delta t\mathbf{L}]_{FD}$ in gridpoint space and the one in spectral space $[1 - \frac{1}{2}\Delta t\mathbf{L}]_{SP}$.

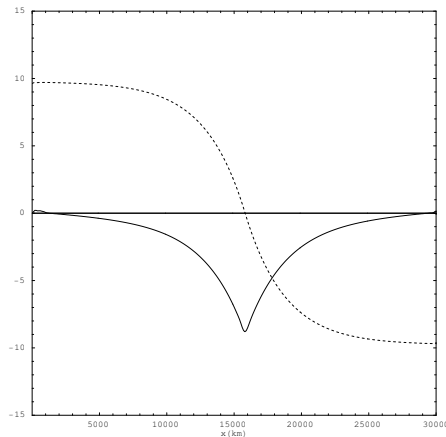
Boyd (2005) proposes a better periodic extension yielding more accurate derivatives than the one in ALADIN, and used here. We expect this to improve.



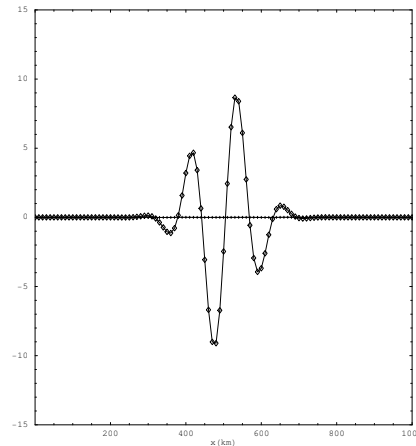
Tests in 1D shallow water



Some tests as they have also been done by McDonald in the shallow-water model, but here in the spectral model.



The adjustment experiment. The gravity waves are leaving the domain correctly without leaving reflections. The final state (see Gill 1982) is correctly reproduced.



A radiation experiment. The initial state is radiated away through the boundaries to infinity.



New approach to LBC's



Conclusions and outlook

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- Renewed optimism to find alternatives for the Davies scheme in spectral models.

